



# PRONTO

Productivity, Non-Tariff  
Measures and Openness

# PRONTO

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## Abstract

In this paper we provide insights into the impact of NTMs on aggregate country and regional productivity. More specifically, we first develop a model characterized by costly trade, love of variety, heterogeneous firms, labour mobility as well as endogenous markups and productivity. We subsequently quantify the model using goods and services trade data as well as GDP and population for European Economic Area (EEA) regions plus other OECD countries. We finally assess the importance of NTMs for productivity, markups, wages and population by performing a series of counterfactual experiments. More specifically, we evaluate the impact of implementing the Transatlantic Trade and Investment Partnership (TTIP) between the EEA and the US. We also perform an additional counterfactual to further isolate the role of NTMs: the exit of the UK from the EEA.



# Estimating the costs and gains of TTIP and BREXIT for EU regions\*

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## Abstract

In this paper we provide insights into the impact of NTMs on aggregate country and regional productivity. More specifically, we first develop a model characterized by costly trade, love of variety, heterogeneous firms, labour mobility as well as endogenous markups and productivity. We subsequently quantify the model using goods and services trade data as well as GDP and population for European Economic Area (EEA) regions plus other OECD countries. We finally assess the importance of NTMs for productivity, markups, wages and population by performing a series of counterfactual experiments. More specifically, we evaluate the impact of implementing the Transatlantic Trade and Investment Partnership (TTIP) between the EEA and the US. We also perform an additional counterfactual to further isolate the role of NTMs: the exit of the UK from the EEA.

**Keywords:** firm heterogeneity; endogenous markups; labour mobility; regions; gravity equation; non-tariff measures; TTIP; Brexit

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# 1 Introduction

The latter half of the 20th century saw a successful international effort to reduce tariffs. These achievements, however, were undone by the subsequent proliferation of non-tariff measures (NTMs) to limit international trade and investment. These measures take a variety of forms and include safety regulations, environmental standards, and corporate tax incentives, all of which influence both trade and investment. Within this context the EU funded research project Productivity, Non-Tariff Measures and Openness (PRONTO) brings together a team of world-class researchers from academia, policy organizations, and the private sector to offer a comprehensive and unified approach to describing and measuring these NTMs and their impact on a variety of social outcomes. PRONTO promises new and better data, better methodologies, and better understanding of the impact of NTMs on international investment and trade. Emphasis is placed on policy relevance and data availability.

In this paper we provide insights into the impact of NTMs on aggregate country and regional productivity as well as on population movements. More specifically, we first develop a model, drawing upon Behrens et al. (2014) and Behrens et al. (2017), characterized by costly trade, love of variety, heterogeneous firms, labour mobility as well as endogenous markups and productivity. We subsequently quantify the model using goods and services trade data as well as GDP and population for European Economic Area (EEA) regions/countries plus other OECD countries: Australia, Canada, Chile, Israel, Japan, Korea, Mexico, New Zealand, Turkey and the US. In the first part of our analysis we quantify our model and do counterfactual analysis at the country-level for both EEA and non-EEA countries. In the second part of our analysis, we break down EEA countries into the corresponding NUTS-2 regions. We finally assess the importance of NTMs for productivity, markups, population and wages by performing a series of counterfactual experiments. More specifically, we evaluate the impact of implementing the Transatlantic Trade and Investment Partnership (TTIP) between the EEA and the US.

We separately consider a liberalization of trade in goods and a liberalization of trade in services (as well as a joint liberalization) with the latter being a much cleaner instance in which NTMs represent the main existing obstacle to international trade. We find that a liberalization of trade in services will have stronger impacts than a liberalization of trade in goods on EEA countries' productivity. However, gains (and

losses) remain modest and in most cases below 1%. Interestingly, countries in the core of the EEA (Germany, Belgium, the Netherlands, etc.) will mainly loose from TTIP while peripheral countries will gain. At the same time, large city-regions (Paris, London) tend to gain less/lose more from deeper service trade integration. The reason is that their large size confer them an advantage that is larger the harder it is to trade. As for population changes, they roughly mirror the pattern of productivity changes and are overall modest. We also perform an additional counterfactual to further isolate the role of NTMs: the exit of the UK from the EEA (Brexit). When focusing on trade in services, we find in this scenario sizeable losses for many EEA countries and in particular for the UK and Ireland (about -1.5% productivity each and with a decrease in population of respectively 1.12% and 1.35%). Furthermore, our results suggest changes induced by Brexit are likely to favor the larger city regions at the expense of smaller regions.

The building blocks of our analysis are the models developed in Behrens et al. (2014) and Behrens et al. (2017). As stated in Behrens et al. (2014), many general equilibrium models of international trade yield equivalent results about the aggregate impacts of trade liberalization for welfare and trade flows as captured by the gravity equation (Arkolakis *et al.*, 2012). However, models differ in their specific predictions along which margins an economy adjusts to freer trade. Recent workhorse frameworks have focused on combinations of wages, productivity, and consumption diversity as adjustment mechanisms, triggered by firm selection and market share reallocations. Yet, those models do not come to grips with the fact that trade integration also changes firms' price-cost margins.

In this respect there has been vastly growing empirical interest in markups recently, and important contributions by De Loecker (2011), De Loecker *et al.* (2016), Feenstra and Weinstein (2017), Simonovska (2015), and others, have established some basic facts: (i) markups differ substantially across firms even within industries, and firms with lower marginal costs tend to charge higher markups; (ii) firms apply different markups across different markets; and (iii) trade integration affects price-cost margins. The main contribution of Behrens et al. (2014) is to develop a general equilibrium quantifiable model of trade under monopolistic competition with variable demand elasticity, heterogeneous firms, and multiple asymmetric countries. Wages, productivity, and consumption diversity are all endogenously determined, and in line with the facts (i)–(iii), markups differ across firms and across markets, and respond to trade integration. We use this model in our analysis and further

allow for mobility of workers across space along the lines of Behrens et al. (2017).

The remainder of this paper is structured as follows. Section 2 develops the model and analyzes its equilibrium properties. We lay out our model quantification procedure in Section 3. In Section 4, we then run different TTIP counterfactuals to quantify the impacts of (i) deeper goods-trade integration, (ii) deeper service-trade integration, and (iii) both types of integration. We also consider, as an additional counterfactual, the exit of the UK from the EEA (Brexit). Last, Section 5 discusses the policy relevance of our finding and concludes. Technical details and proofs are relegated to the Appendix.

## 2 Model

Our model builds on Behrens, Mion, Murata, and Südekum (2014, 2017). There are  $r = 1, 2, \dots, K$  countries or regions. For simplicity, we henceforth always use the term regions. Region  $r$  has a population of  $L_r$  workers who are also consumers. Each individual supplies inelastically one unit of labor. Labor is the only factor of production, and it is supplied locally (i.e., there is no cross-regional commuting). However, we assume that individuals are mobile across countries and regions, i.e., they are free to pick their place of residence.

We first set up the model in Sections 2.1 and 2.2, and then analyze the firm-level outcomes and the ‘short run’ equilibrium — when people are immobile and do not relocate across regions — in Section 2.3. We spell out the details concerning labor mobility in Section 2.4.

### 2.1 Preferences and demands

There is a continuum of horizontally differentiated varieties of final consumption goods and services. Consumers have identical preferences that display ‘love of variety’ and give rise to demands with variable elasticity. One key property of our model is that the marginal utility at zero consumption is bounded. Hence, consumers will not demand varieties for which the price (including trade costs) is too high. Those varieties are not traded across regions/countries, as is often the case for numerous services. Our model thus naturally applies to the analysis of the aggregate economy in which goods and services co-exist.

Let  $p_{sr}(i)$  and  $q_{sr}(i)$  denote the price and the per capita consumption of variety  $i$  when it is produced in region  $s$  and consumed in region  $r$ . The utility maximization problem of a representative individual in region  $r$  is given by:

$$\max_{q_{sr}(j), j \in \Omega_{sr}} U_r \equiv \sum_s \int_{\Omega_{sr}} [1 - e^{-\alpha q_{sr}(j)}] dj \quad \text{s.t.} \quad \sum_s \int_{\Omega_{sr}} p_{sr}(j) q_{sr}(j) dj = E_r, \quad (1)$$

where  $\alpha > 0$  is a utility parameter, and where  $\Omega_{sr}$  denotes the endogenously determined set of varieties produced in  $s$  and consumed in  $r$ . As shown in Appendix A.1, solving (1) yields the following demand functions:

$$q_{sr}(i) = \frac{E_r}{N_r^c \bar{p}_r} - \frac{1}{\alpha} \left\{ \ln \left[ \frac{p_{sr}(i)}{N_r^c \bar{p}_r} \right] + h_r \right\}, \quad \forall i \in \Omega_{sr}, \quad (2)$$

where  $N_r^c$  is the mass of varieties consumed in region  $r$ , and

$$\bar{p}_r \equiv \frac{1}{N_r^c} \sum_s \int_{\Omega_{sr}} p_{sr}(j) dj \quad \text{and} \quad h_r \equiv - \sum_s \int_{\Omega_{sr}} \ln \left[ \frac{p_{sr}(j)}{N_r^c \bar{p}_r} \right] \frac{p_{sr}(j)}{N_r^c \bar{p}_r} dj$$

denote the average price and the differential entropy of the price distribution, respectively.

As explained before, demand does not need to be positive if the price charged for the variety is too high. Formally, as can be seen from (2), the demand for the local variety  $i$  (resp., the distant variety  $j$ ) is positive if and only if the price of variety  $i$  (resp., variety  $j$ ) is lower than some *choke price*  $p_r^d$ :  $q_{rr}(i) > 0$  if and only if  $p_{rr}(i) < p_r^d$ ; and  $q_{sr}(j) > 0$  if and only if  $p_{sr}(j) < p_r^d$ , where  $p_r^d \equiv N_r^c \bar{p}_r e^{\alpha E_r / (N_r^c \bar{p}_r) - h_r}$  depends on the price aggregates  $\bar{p}_r$  and  $h_r$ .

Using the definition of the choke price allows us to express the demands for local and distant varieties concisely as follows:

$$q_{rr}(i) = \frac{1}{\alpha} \ln \left[ \frac{p_r^d}{p_{rr}(i)} \right] \quad \text{and} \quad q_{sr}(j) = \frac{1}{\alpha} \ln \left[ \frac{p_r^d}{p_{sr}(j)} \right]. \quad (3)$$

The price elasticity of the local variety  $i$  (resp., the distant variety  $j$ ) is given by  $1/[\alpha q_{rr}(i)]$  (resp.,  $1/[\alpha q_{sr}(j)]$ ). Thus, if individuals consume more of those varieties, which is for instance the case when their expenditure increases, they become less price sensitive (see, e.g., Simonovska, 2015). Hence, the model allows us to take into account the fact that richer consumers are less price sensitive than poorer consumers.

Last, since  $e^{-\alpha q_{sr}(j)} = p_{sr}(j)/p_r^d$ , the indirect utility in region  $r$  is given by

$$U_r = N_r^c - \sum_s \int_{\Omega_{sr}} \frac{p_{sr}(j)}{p_r^d} dj = N_r^c \left( 1 - \frac{\bar{p}_r}{p_r^d} \right). \quad (4)$$

Expression (4) will prove useful to compute the equilibrium utility in the subsequent analysis and to assess the welfare consequences of changing trade costs.

## 2.2 Technology and market structure

The production side of the model features heterogeneous firms as in Melitz (2003) and Melitz and Ottaviano (2008). Prior to production, firms decide in which region they enter and they engage in research and development. The labor market in each region is perfectly competitive, so that all firms take the wage rate as given. Entry in region  $r$  requires a fixed amount  $F_r$  of labor paid at the market wage  $w_r$ . Each firm  $i$  that enters in region  $r$  discovers its marginal labor requirement  $m_r(i) \geq 0$  only after making this irreversible entry decision. We assume that  $m_r(i)$  is drawn from a known, continuously differentiable distribution  $G_r$ .<sup>1</sup> In what follows we assume, for simplicity, that firms' productivity draws  $1/m$  follow a Pareto distribution

$$G_r(m) = \left( \frac{m}{m_r^{\max}} \right)^k,$$

with region-specific upper bounds,  $m_r^{\max} > 0$ , and a common shape parameter,  $k \geq 1$ . The Pareto distribution has been extensively used in the previous literature on heterogeneous firms (e.g., Bernard et al., 2007b; Helpman et al., 2008; Melitz and Ottaviano, 2008). It provides a good approximation of the distribution of firm sizes.

Shipments from region  $r$  to region  $s$  are subject to trade costs  $\tau_{rs} > 1$  for all  $r$  and  $s$ , which firms incur in terms of labor. Put differently, the firm has to hire  $\tau_{rs} - 1$  additional workers in order to ship the good from region  $r$  to region  $s$ . Those additional costs include, e.g., transportation costs of the good per se, but also different non-tariff barriers (NTB) that will be the key focus of our subsequent quantitative analysis. Observe that these NTBs can differ across goods and services.

Since entry costs are sunk, firms will survive (i.e., operate) provided they can charge prices  $p_{sr}(i)$  above marginal costs  $\tau_{rs}m_r(i)w_r$  in at least one region. This

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<sup>1</sup>Differences in the sunk entry costs  $F_r$  and the productivity distributions  $G_r$  across regions/countries thus reflect production amenities such as startup costs, technology, and local knowledge that are only partly transferable across space, as well as differences in the institutional environments in which firms operate. Firms take those differences into account when making their entry decisions. Note that differences in start-up costs and institutions across countries are large (see, e.g., the World Bank's "Doing business" report; World Bank, 2016). Our model allows us to recover an implicit measure of these technological and institutional differences across regions/countries in equilibrium.

usually includes the region the firm is located in, but the model allows for situations where a firm can survive only because of its distant demand and does not sell anything to its local market. While this situation seems not very relevant in an international context, it clearly is at smaller geographic scales such as the interregional context that we will focus on in what follows. The surviving firms produce in the region where they enter. We assume that firms do not relocate, i.e., once location choices have been made there is no relocation. Adding relocation makes the model complicated since it requires to deal with the spatial sorting of firms along productivity (see, e.g., Gaubert, 2015, for a model dealing with that question).

In line with empirical evidence, we assume that product markets are segmented, i.e., resale or third-party arbitrage is sufficiently costly, so that firms are free to price discriminate between regions. This is even a feature of a priori integrated economic areas such as the EU. There is substantial evidence that international product markets are segmented so that firms can do ‘pricing-to-market’ (see, e.g., Haskel and Wolf, 2001; Simonovska, 2015). While regions are a priori more integrated than countries, deviations from the law-of-one-price also apply there, as, e.g., seen from interregional border effects (Wolf, 2000).

The operating profit of a firm  $i$  located in region  $r$  is then as follows:

$$\pi_r(i) = \sum_s \pi_{rs}(i) = \sum_s L_s q_{rs}(i) [p_{rs}(i) - \tau_{rs} m_r(i) w_r], \quad (5)$$

where  $\pi_{rs}(i)$  is the operating profit in market  $s$ , and  $q_{rs}(i)$  is given by (3). Each surviving firm maximizes (5) with respect to its prices  $p_{rs}(i)$  separately. Because there is a continuum of firms, no individual firm has any impact on  $p_r^d$ , so that the first-order conditions for (operating) profit maximization are given by:

$$\ln \left[ \frac{p_s^d}{p_{rs}(i)} \right] = \frac{p_{rs}(i) - \tau_{rs} m_r(i) w_r}{p_{rs}(i)}, \quad \forall i \in \Omega_{rs}. \quad (6)$$

A price distribution satisfying (6) almost everywhere is called a *price equilibrium*. Equations (3) and (6) imply that  $q_{rs}(i) = (1/\alpha)[1 - \tau_{rs} m_r(i) w_r / p_{rs}(i)]$ . Thus, the minimum output that a firm in  $r$  may sell in market  $s$  is given by  $q_{rs}(i) = 0$  at  $p_{rs}(i) = \tau_{rs} m_r(i) w_r$ . This, by (6), implies that  $p_{rs}(i) = p_s^d$ . Hence, a firm located in  $r$  with draw  $m_{rs}^x \equiv p_s^d / (\tau_{rs} w_r)$  is just indifferent between selling and not selling to  $s$ , whereas all firms in  $r$  with draws below  $m_{rs}^x$  are productive enough to sell to  $s$ . In what follows, we refer to  $m_{ss}^x \equiv m_s^d$  as the *local cutoff* in region  $s$ , whereas  $m_{rs}^x$

with  $r \neq s$  is the ‘*export*’ cutoff from region  $r$  to region  $s$ . Export and local cutoffs are linked by the following relationship:

$$m_{rs}^x = \frac{\tau_{ss}}{\tau_{rs}} \frac{w_s}{w_r} m_s^d. \quad (7)$$

Expression (7) reveals how trade costs and wage differences affect firms’ abilities to break into different markets. In particular, when wages are the same in the two regions ( $w_r = w_s$ ) and trade is costless ( $\tau_{ss} = 1$ ), all export cutoffs must fall short of the local cutoffs since  $\tau_{rs} > 1$ . Breaking into market  $s$  is then always harder for firms in  $r \neq s$  than its local competitors in  $s$ , which is the standard case considered in the literature (e.g., Melitz, 2003; Melitz and Ottaviano, 2008).<sup>2</sup>

Given the cutoffs (7) and the mass of entrants  $N_r^E$ , only  $N_r^p = N_r^E G_r(\max_s \{m_{rs}^x\})$  firms survive, namely those which are productive enough to sell at least in one market (which, as mentioned before, need not be their local market). The mass of varieties *consumed* in region  $r$  is given by

$$N_r^c = \sum_s N_s^E G_s(m_{sr}^x), \quad (8)$$

which is the mass of all firms that are productive enough to sell to market  $r$ . Welfare changes in region  $r$  will be intimately linked to changes in  $N_r^c$  because consumers value variety in consumption.

### 2.3 Equilibrium with immobile labor

We now solve for the general equilibrium of our multi-regional trade model with heterogeneous firms. To do so, we first need to derive the firm-level outcomes in terms of prices, quantities, and profits. We relegate that part of the analysis and the corresponding technical details and expressions to Appendix A.2. We next need to consider three sets of equilibrium conditions. First, for each region, zero expected profit holds. Using equation (5), the zero expected profit condition (henceforth, ZEP) is given by

$$\sum_s L_s \int_0^{m_{rs}^x} [p_{rs}(m) - \tau_{rs} m w_r] q_{rs}(m) dG_r(m) = F_r w_r. \quad (9)$$

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<sup>2</sup>However, in the presence of wage differences and intra-regional trade costs  $\tau_{rr}$ , the local cutoff need not be larger than the export cutoff in equilibrium. The usual ranking  $m_s^d > m_{rs}^x$  prevails only when  $\tau_{ss} w_s < \tau_{rs} w_r$ .

Second, since there is no interregional commuting, local labor markets clear in each region. The labor market clearing condition (henceforth, LMC) requires that

$$N_r^E \left[ \sum_s L_s \tau_{rs} \int_0^{m_{rs}^x} m q_{rs}(m) dG_r(m) + F_r \right] = L_r. \quad (10)$$

Condition (10) states that the labor hired by firms to produce for both the local and the different distant markets, including the labor used to overcome trade costs and the labor hired to pay for the sunk entry costs (irrespective of whether the firm survives subsequently or not), sums to the regional labor endowment. The latter will be endogenously determined by the location decisions of interregionally mobile individuals.

Last, trade must balance for each region, which is equivalent to saying that each consumer's budget constraint is satisfied with equality in each region. The trade balance condition (henceforth, TBC) for region  $r$  requires that the total value of exports equals the total value of imports, and it is given by

$$N_r^E \sum_{s \neq r} L_s \int_0^{m_{rs}^x} p_{rs}(m) q_{rs}(m) dG_r(m) = L_r \sum_{s \neq r} N_s^E \int_0^{m_{sr}^x} p_{sr}(m) q_{sr}(m) dG_s(m). \quad (11)$$

The  $3 \times K$  general equilibrium conditions (9)–(11) depend on  $3 \times K$  unknowns: the wages  $w_r$ , the masses of entrants  $N_r^E$ , and the local cutoffs  $m_r^d$ . Once the local cutoffs and the wages have been determined, the export cutoffs  $m_{rs}^x$  can be computed by using (7). Before proceeding, we simplify the general equilibrium conditions by using the Pareto parametrization and the results from Appendices A.2 and A.3. Using those results, the ZEP, LMC and TBC conditions can be rewritten as follows:

$$\mu_r^{\max} = \sum_s L_s \tau_{rs} \left( \frac{\tau_{ss} w_s}{\tau_{rs} w_r} m_s^d \right)^{k+1}, \quad (12)$$

$$N_r^E \left[ \frac{\kappa_1}{\alpha (m_r^{\max})^k} \sum_s L_s \tau_{rs} \left( \frac{\tau_{ss} w_s}{\tau_{rs} w_r} m_s^d \right)^{k+1} + F_r \right] = L_r, \quad (13)$$

$$\frac{N_r^E w_r}{(m_r^{\max})^k} \sum_{s \neq r} L_s \tau_{rs} \left( \frac{\tau_{ss} w_s}{\tau_{rs} w_r} m_s^d \right)^{k+1} = L_r \sum_{s \neq r} \tau_{sr} \frac{N_s^E w_s}{(m_s^{\max})^k} \left( \frac{\tau_{rr} w_r}{\tau_{sr} w_s} m_r^d \right)^{k+1}, \quad (14)$$

where  $\mu_r^{\max} \equiv [\alpha F_r (m_r^{\max})^k] / \kappa_2$  is a bundle of parameters that captures 'technological possibilities'. Note that  $\mu_r^{\max}$  is region-specific and depends on both the sunk entry costs  $F_r$  and the upper bounds of the underlying productivity distribution

$m_r^{\max}$ . Thus, this bundle of parameters captures the local production amenities that are not transferable across space. It also subsumes aspects of the institutional environment of the region/country.

Combining (12) and (13), we obtain

$$N_r^E = \frac{\kappa_2}{\kappa_1 + \kappa_2} \frac{L_r}{F_r}, \quad (15)$$

which implies that more firms choose to enter in larger markets and in markets with lower entry requirements. Adding the term in  $r$  that is missing on both sides of (14), and using (12) and (15), we then obtain the following relationship:

$$\frac{1}{(m_r^d)^{k+1}} = \sum_s L_s \tau_{rr} \left( \frac{\tau_{rr}}{\tau_{sr}} \frac{w_r}{w_s} \right)^k \frac{1}{\mu_s^{\max}}. \quad (16)$$

The  $2 \times K$  conditions (12) and (16), obtained by substituting out the equilibrium masses of entrants  $N_r^E$ , summarize how wages and cutoffs are related in general equilibrium, given the regional population sizes, technological possibilities, and trade costs.

Using these expressions, we can furthermore show that — in equilibrium — the mass of varieties consumed in region  $r$  is inversely proportional to the domestic cutoff, while the (expenditure share) weighted average of markups that consumers face is proportional to the local cutoff (see Appendix A.4 for the derivations):

$$N_r^c = \frac{1}{\kappa_1 + \kappa_2} \frac{\alpha}{\tau_{rr} m_r^d}, \quad (17)$$

$$\bar{\Lambda}_r^c \equiv \frac{\sum_s N_s^E \int_0^{m_{sr}^x} \frac{p_{sr}(m) q_{sr}(m)}{E_r} \Lambda_{sr}(m) dG_s(m)}{\sum_s N_s^E G_s(m_{sr}^x)} = \frac{\kappa_3 \tau_{rr} m_r^d}{\alpha}, \quad (18)$$

where  $\kappa_1$ ,  $\kappa_2$ , and  $\kappa_3$  are positive constants that depend only on the common shape parameter  $k$  of the Pareto distribution.<sup>3</sup>

Under the Pareto parametrization, average productivity in region  $r$  is simply

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<sup>3</sup>It can be seen from (17) and (18) that there are pro-competitive effects in our model, since  $\bar{\Lambda}_r^c = [\kappa_3/(\kappa_1 + \kappa_2)](1/N_r^c)$  decreases with the mass of competing firms in region  $r$ .

proportional to the inverse of the local cutoff:<sup>4</sup>

$$A_r = \frac{1}{G_r(m_j^d)} \int_0^{m_r^d} \frac{1}{m} dG_r(m) = \frac{k_r}{k_r - 1} \frac{1}{m_r^d}. \quad (19)$$

Finally, the indirect utility in region  $r$  can be expressed as

$$U_r = \left[ \frac{1}{(\kappa_1 + \kappa_2)(k + 1)} - 1 \right] \frac{\alpha}{\tau_{rr} m_r^d} = \left[ \frac{1}{(\kappa_1 + \kappa_2)(k + 1)} - 1 \right] \frac{\kappa_3}{\bar{A}_r^c}, \quad (20)$$

which implies that tougher selection (lower  $m_r^d$ ) and fiercer competition (lower  $\bar{A}_r^c$ ) both translate into higher welfare in region  $r$ .<sup>5</sup>

## 2.4 Labor mobility and spatial equilibrium

Until now, we have taken the regional population sizes  $L_r$  as given. We now endogenize them by allowing individuals to move across regions to exploit differences in real incomes. To this end, we introduce taste heterogeneity in residential locations into our model. This is done for two reasons. First, individuals in reality choose their location not only based on wages, prices, and consumption diversity that result from market interactions, but also based on non-market features such as amenities (e.g., climate or landscape) and local social networks. The relatively low interregional mobility in Europe suggests that regional attachment is an important feature of individual location choices, and regional amenities and social networks certainly play a key role there (e.g., Faini et al., 1997; Faini, 1999). Second, individuals do not necessarily react in the same way to regional gaps in wages and cost-of-living. Such taste heterogeneity offsets the extreme — and counterfactual —

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<sup>4</sup>Alternatively, we can use the average (variable) labor productivity

$$\tilde{A}_j = \left[ \int_0^{m_j^d} q_j(m) dG_j(m) \right] \cdot \left[ \int_0^{m_j^d} mq_j(m) dG_j(m) \right]^{-1} = \left( \frac{k_j + 1}{k_j} \right)^2 \frac{1}{m_j^d},$$

which generates quantitatively the same percentage productivity changes as  $A_j$ .

<sup>5</sup>Alternatively, we have  $U_r = [1/(k + 1) - (\kappa_1 + \kappa_2)]N_r^c$ , i.e., the indirect utility is proportional to the mass of varieties consumed. The welfare gains come from imported varieties (Broda and Weinstein, 2006), as the mass of domestic varieties  $N_r^E G_r(m_r^d)$  decreases when trade integration reduces the cutoff  $m_r^d$ . This finding is in line with those by Feenstra and Weinstein (2017), who show that new import varieties have contributed to us welfare gains even when taking into account the displaced domestic varieties.

outcome that often arises in typical agglomeration models with mobile individuals, namely that *all* mobile economic activity concentrates in a single region (Tabuchi and Thisse, 2002; Murata, 2003).

We assume that the location choice of an individual  $\ell$  is based on a linear random utility  $V_r^\ell = U_r + A_r + \xi_r^\ell$ , where  $U_r$  is given by (20) and  $A_r$  subsumes region-specific amenities that are equally valued by all individuals. We usually do not observe  $A_r$  (or observe it only very imperfectly). The random variable  $\xi_r^\ell$  captures idiosyncratic taste differences in residential location, subsuming many unobserved features such as social networks, amenities, and family ties. Following McFadden (1974), we assume that the  $\xi_r^\ell$  are i.i.d. across individuals and regions according to a double exponential distribution with zero mean and variance equal to  $\pi^2 \beta^2 / 6$ , where  $\beta$  is a positive constant. Since  $\beta$  has a positive relationship with variance, the larger the value of  $\beta$ , the more heterogeneous are the consumers' attachments to each region. This makes, everything else equal, the population less sensitive to differences in regional utility differences that stem from differences in prices and wages.

Given the population distribution, an individual's probability of choosing region  $r$  can then be expressed as a logit form:

$$\mathbb{P}_r = \Pr \left( V_r^\ell > \max_{s \neq r} V_s^\ell \right) = \frac{\exp((U_r + A_r)/\beta)}{\sum_{s=1}^K \exp((U_s + A_s)/\beta)}. \quad (21)$$

For the distribution of population across regions to be non-degenerated, we assume that  $\beta > 0$  in the subsequent analysis.<sup>6</sup> A *spatial equilibrium* is defined as a distribution of population across regions such that

$$\mathbb{P}_r = \frac{L_r}{\sum_{s=1}^K L_s}, \quad \forall r. \quad (22)$$

In words, a spatial equilibrium is a fixed point where the choice probability of each region is equal to that region's share of the economy's total population. This is a direct consequence of the law of large numbers. In theory, there can be multiple regional population distributions satisfying (22). However, this is not an issue given the aim of our paper. Indeed, in Section 3.3, when we fit our model to data, we plug the observed regional population shares into the right-hand side of (22) and

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<sup>6</sup>If  $\beta \rightarrow 0$ , which corresponds to the case without taste heterogeneity, people choose their location based only on  $U_r + A_r$ , i.e., they choose the region with the highest  $U_r + A_r$  with probability one. By contrast, if  $\beta \rightarrow \infty$ , individuals choose regions with equal probability  $1/K$ . In that case, regional tastes are extremely heterogeneous, so that  $U_r + A_r$  does not affect location decisions at all.

uniquely back out  $(U_r + A_r)/\beta$  such that this population distribution is a spatial equilibrium.

### 3 Quantification

To take our model to the data, we first derive a system of gravity equations and restate the general equilibrium conditions of the model. The gravity equation is required to estimate the trade frictions for goods and service trade from the data, whereas the general equilibrium conditions are required to take the model structurally to the data and to simulate the counterfactual impacts of the changes in trade barriers.

#### 3.1 Gravity equation system

We now derive a system of gravity equations that will be useful for taking the model to the data. The value of exports from region  $r$  to region  $s$  is given by

$$X_{rs} = N_r^E L_s \int_0^{m_{rs}^x} p_{rs}(m) q_{rs}(m) dG_r(m).$$

Using (7), (A-3), (15), and the Pareto distribution for  $G_r(m)$ , we obtain the following gravity equation:

$$X_{rs} = L_r L_s \tau_{rs}^{-k} \tau_{ss}^{k+1} (w_s/w_r)^{k+1} w_r \left( m_s^d \right)^{k+1} (\mu_r^{\max})^{-1}. \quad (23)$$

As can be seen from (23), the value of shipments depend on bilateral trade costs  $\tau_{rs}$ , internal trade costs in the destination region  $\tau_{ss}$ , origin and destination regional wages  $w_r$  and  $w_s$ , the destination region cutoff  $m_s^d$ , and the origin region's technological possibilities  $\mu_r^{\max}$ . It is also increasing with the destination region's number of consumers,  $L_s$ , and the origin region's labor supply. A higher relative wage  $w_s/w_r$  raises the value of exports as firms in  $r$  face relatively lower production costs, whereas a higher absolute wage  $w_r$  raises the value of exports by increasing export prices  $p_{rs}$ . Furthermore, a larger  $m_s^d$  raises the value of exports since firms located in the destination are on average less productive. Last, a lower  $\mu_r^{\max}$  implies that firms in region  $r$  have higher expected productivity, which raises the value of their exports. From the zcp and the zep conditions, we further obtain the following general

equilibrium conditions:

$$\mu_r^{\max} = \sum_s L_s \tau_{rs} \left( \frac{\tau_{ss} w_s}{\tau_{rs} w_r} m_s^d \right)^{k+1}, \quad (24)$$

$$\frac{1}{(m_r^d)^{k+1}} = \sum_s L_s \tau_{rr} \left( \frac{\tau_{rr} w_r}{\tau_{sr} w_s} \right)^k \frac{1}{\mu_s^{\max}}. \quad (25)$$

The  $2 \times K$  general equilibrium conditions (24) and (25) summarize the interactions between the endogenous variables, namely the  $K$  wages and the  $K$  cutoffs. These conditions are reminiscent of those in Anderson and van Wincoop (2003), who argue that general equilibrium interdependencies need to be taken into account when conducting a counterfactual analysis based on the gravity equation.

Interestingly, the gravity equation system (23)–(25) is, indeed, akin to that in Anderson and van Wincoop (2003). To see this, let  $Y_r = w_r L_r$  be the labor income of region  $r$ . Define the total labor income in all regions as  $Y_w = \sum_r w_r L_r$  and the labor income share of region  $r$  as  $\sigma_r = Y_r / Y_w$ . Also define the multilateral resistance terms as follows:

$$\Phi_r^{-k} = \sigma_r^{k+1} \mu_r^{\max} L_r^{-k-1} \quad (26)$$

$$\Psi_s^{-k} = \sigma_s^{-k} \tau_{ss}^{-k-1} (m_s^d)^{-k-1} L_s^k. \quad (27)$$

Then, our gravity equation system (23)–(25) can be rewritten as follows:

$$X_{rs} = \frac{Y_r Y_s}{Y_w} \left( \frac{\tau_{rs}}{\Phi_r \Psi_s} \right)^{-k} \quad (28)$$

$$\Phi_r^{-k} = \sum_v \sigma_v \left( \frac{\tau_{rv}}{\Psi_v} \right)^{-k} \quad (29)$$

$$\Psi_s^{-k} = \sum_v \sigma_v \left( \frac{\tau_{vs}}{\Phi_v} \right)^{-k}, \quad (30)$$

which is the same as the gravity equation system (9)–(11) in Anderson and van Wincoop (2003), except that their exponent capturing the elasticity of substitution is replaced by the shape parameter  $k$  of the Pareto distributions. Assuming that  $\tau_{rs} = \tau_{sr}$ , i.e., trade costs are symmetric as in Anderson and van Wincoop (2003), we know that (29) and (30) yield a solution  $\Phi_r = \Psi_r$  that solves the equations

$$\Phi_r^{-k} = \sum_v \sigma_v \tau_{rv}^{-k} \Phi_v^k. \quad (31)$$

We will use this property in the subsequent analysis as it greatly simplifies our quantification procedure.

### 3.2 Data

In order to make our model operational we need data on trade costs as well as on GDP and population. In order to recover trade costs we build on a gravity approach consistent with (28) and use data on trade in goods (services) coming from the COM-TRADE (ITS) database provided by the United Nations (Eurostat) for the period 2010-2013. We also consider the usual set of gravity equation covariates provided by the Centre d'Etude Prospectives et d'Informations Internationales (CEPII): distance ( $d_{rs}$ ), an ex-colony dummy ( $Colony_{rs}$ ), a common language dummy ( $Lang_{rs}$ ), a common border dummy ( $Border_{rs}$ ) as well as a dummy indicating whether countries  $r$  and  $s$  belong to the European Economic Area or not ( $EEA_{rs}$ ).

As for population and GDP we borrow this data from the Eurostat Regio Database (for EEA regions) and the World Economic Outlook Database provided by the IMF (for non-EEA countries). Data on population and GDP refers to the year 2014. Countries included in our analysis are all current members of the EEA but Luxembourg plus other OECD countries: Australia, Canada, Chile, Israel, Japan, Korea, Mexico, New Zealand, Turkey and the US. In the first part of our analysis we quantify our model and do counterfactual analysis at the country-level for both EEA and non-EEA countries. In the second part of our analysis, we break down EEA countries into the corresponding NUTS-2 regions. We use the GDP of country/region  $r$  as a measure of  $Y_r$ , population as a measure of  $L_r$  and GDP per capita as a proxy for  $w_r$ .

### 3.3 Quantification procedure

We now explain the numerical procedure that we implement to calibrate the model to the initial equilibrium. The steps of our numerical procedure work as follows.

1. We specify trade costs as  $\tau_{rs} \equiv d_{rs}^\gamma e^{\theta_1 EEA_{rs}} e^{\theta_2 Colony_{rs}} e^{\theta_3 Lang_{rs}} e^{\theta_4 Border_{rs}}$ . We are particularly interested in the coefficient corresponding to membership of the EEA:  $\theta_1$
2. Given our specification of trade costs  $\tau_{rs}$ , the gravity equation (28) can be rewritten in log-linear stochastic form as follows:

$$\ln X_{rs} = c - k \ln \tau_{rs} + k \ln \Phi_r + k \ln \Psi_s + \varepsilon_{rs}, \quad (32)$$

where  $\varepsilon_{rs}$  is an error term with the usual properties. We estimate (32) at the *country-level* for our group of EEA and non-EEA countries. We do this in a

way that is consistent with (28) by using origin and destination fixed effects to control for multilateral resistance terms  $\Phi_r$  and  $\Psi_s$ .<sup>7</sup> In Behrens et al. (2014), we also quantify the value of  $k$ . To this end, we compute the productivity advantage of US exporters from a random sample of firms drawn from the fitted productivity distributions of our model. We repeat this procedure for different values of  $k$  until our sample matches the 33% productivity advantage of US exporters in 1992, which is reported by Bernard et al. (2003). See Behrens et al. (2014) for details. Here, we use their value of  $\hat{k} = 8.5$  in the analysis.

3. Using estimates from the log-linear stochastic gravity regression (32), we construct trade costs. In the first part of our analysis we quantify our model and do counterfactual analysis at the country-level for both EEA and non-EEA countries and so compute trade costs across countries. In the second part of our analysis, we break down EEA countries into the corresponding NUTS-2 regions and thus compute trade costs across EEA regions and non-EEA countries.<sup>8</sup>

Trade costs enter the gravity equation (28) as  $\tau_{rs}^{-k} \equiv \phi_{rs} \in (0, 1)$  where  $\phi_{rs}$  is an inverse measure of trade costs, i.e., the freeness of trade, and so we actually compute a measure of freeness of trade corresponding to the initial trading equilibrium. We do this separately for goods and services gravity regressions and then average the two sets of  $\phi_{rs}$  by using world trade shares of trade in goods (75%) and services (25%).

4. We observe the initial values of regional/national populations  $L_r^0$  and GDP  $w_r^0 L_r^0$  from the data and so we can compute income shares  $\sigma_r^0$ . Since our trade costs are symmetric, we solve the system

$$\Phi_r^{-k} = \sum_v \sigma_v^0 \tau_{rv}^{-k} \Phi_v^k, \quad (33)$$

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<sup>7</sup>We do not make use of the full general equilibrium system. Doing so makes actually little difference. See Behrens et al. (2014) for an estimation of the full system using US-Canada data.

<sup>8</sup>We assign trade costs between, for example, any UK NUTS-2 region and the US to be the same and equal to the trade costs between the UK and the US computed from (32). As for trade costs between the NUTS-2 regions of, for example, London and Rome we use country-level values for variables other than distance while for the latter we actually use the distance between London and Rome, along with our estimate of  $\gamma$ , to compute the distance-related component of trade costs.

for the  $\Phi_r$  terms. Call that solution  $\widehat{\Phi}_r^0$ , where the hat stands for ‘quantified’ and where 0 is the initial iteration.

5. Using (26) and (27), we solve

$$\begin{aligned} (\widehat{\Phi}_s^0)^{-k} &= (\sigma_s^0)^{-k} \tau_{ss}^{-k-1} (m_s^d)^{-k-1} (L_s^0)^k \\ (\widehat{\Phi}_r^0)^{-k} &= (\sigma_r^0)^{k+1} \mu_r^{\max} (L_r^0)^{-k-1} \end{aligned}$$

for the cutoff  $(\widehat{m}_s^d)^0$  and the unobserved upper bounds  $\widehat{\mu}_r^{\max}$ .

6. Using  $(\widehat{m}_s^d)^0$ , we use (20) to compute the indirect utility due to the consumption of the differentiated varieties:

$$\widehat{U}_r^0 = \frac{\alpha}{\tau_{rr}} \left[ \frac{1}{(k+1)(\kappa_1 + \kappa_2)} - 1 \right] \frac{1}{(\widehat{m}_r^d)^0} \propto \frac{1}{\tau_{rr}} \frac{1}{(\widehat{m}_r^d)^0}. \quad (34)$$

We compute this up to a scaling that does not matter for the equilibrium (the level of utility is immaterial, and it cannot be meaningfully used).

7. Finally, we calibrate the model to replicate the initial distribution of population as an equilibrium. To this end, we use the initial populations and solve the logit equation system (21) as follows:

$$\frac{L_r^0}{\sum_s L_s^0} = \frac{\exp(D_r)}{\sum_s \exp(D_s)}, \quad (35)$$

for the  $D_r$  terms, using a linear random utility (LRU) as explained in Section 2.4. Using the quantified values of  $\widehat{D}_r^0$  and  $\widehat{U}_r^0$  we have  $\widehat{A}_r = \widehat{D}_r^0 - \widehat{U}_r^0$ . These are the (observed and unobserved) amenities that sustain the spatial equilibrium that we observe from the data. These amenities will be held fixed in the counterfactuals, just as the upper bounds  $\widehat{\mu}_r^{\max}$  are held fixed. Note that we use equal weighting of utility and amenities in what follows. This has no strong implications for our results. We could use different weighting schemes, notably ones that are estimated using available amentiy data and geological instruments to deal with potential problems of reverse causality (see Behrens et al., 2017).

The foregoing seven steps allow us to bring the model to the data and to replicate the observed regional population distribution as a spatial general equilibrium of the model.

### 3.4 Gravity estimation results

Table 1 below reports *country-level* gravity estimation results for goods (column 1) and services (column 2). As one can notice all coefficients are significant and have the usual sign and magnitude. In particular, the EEA dummy is positive and significant for both goods and service while being larger in the latter. Using estimates from Table 1 we construct trade costs corresponding to the initial trading equilibrium. In the first part of our analysis, we quantify our model and do counterfactual analysis at the country-level for both EEA and non-EEA countries and so we use trade costs at the country-level. In the second part of our analysis, we break down EEA countries into the corresponding NUTS-2 regions and so compute trade costs across EEA regions and non-EEA countries. In particular, we assign trade costs between, for example, any UK NUTS-2 region and the US to be the same and equal to the trade costs between the UK and the US computed from (32). As for trade costs between the NUTS-2 regions of, for example, London and Rome we use country-level values for variables other than distance while for the latter we actually use the distance between London and Rome, along with our estimate of  $\gamma$ , to compute the distance-related component of trade costs.

We do this separately for goods and services gravity regressions and then average the two sets of  $\phi_{rs}$  by using world trade shares of trade in goods (75%) and services (25%). Then, we also construct the counterfactual freeness  $\tilde{\phi}_{rs}$  that would prevail in each of the counterfactual scenarios we consider. In what follows, the counterfactuals we consider are those where trade (either in goods, or in services, or both) between the US and the EU would not be subject to additional non-tariff barriers (which would be the case if TIPP ever comes into effect). To implement this, we update the dummy variable  $EEA_{rs}$  by imposing it is equal to 1 if  $r$  and  $s$  belong to the EEA+US set and zero otherwise. With the counterfactual  $\widetilde{EEA}_{rs}$  in our hands we then compute the counterfactual freeness  $\tilde{\phi}_{rs}$ . When we consider, as an additional counterfactual, the exit of the UK from the EEA we employ a similar strategy by removing the UK from the set of EEA countries and updating the dummy  $EEA_{rs}$ , and so the measure of trade freeness, accordingly.

Table 1: Gravity estimation results for goods (column 1) and services (column 2)

	Goods	Services
Distance	-1.411 <sup>a</sup> (0.042)	-1.111 <sup>a</sup> (0.050)
EEA dummy	0.273 <sup>a</sup> (0.093)	0.337 <sup>b</sup> (0.160)
Colony dummy	0.169 <sup>c</sup> (0.101)	0.581 <sup>a</sup> (0.088)
Language dummy	0.348 <sup>a</sup> (0.061)	0.118 <sup>c</sup> (0.067)
Border dummy	0.326 <sup>a</sup> (0.079)	0.447 <sup>a</sup> (0.086)
Year dummies	Yes	Yes
Origin and Destination dummies	Yes	Yes
Observations	5,928	3,836
$R^2$	0.891	0.873

Robust standard errors in parentheses. <sup>abc</sup> indicate the significance of the coefficient, <sup>a</sup>  $p < 0.01$ , <sup>b</sup>  $p < 0.05$ , <sup>c</sup>  $p < 0.1$ .

## 4 Counterfactuals

We now run a series of counterfactual exercises to gauge the potential impact of freer trade in (i) services, (ii) goods, or (iii) both with the US on EU countries and their regions. We also consider, as an additional counterfactual, the exit of the UK from the EEA (Brexit). To this end, we shock the initial equilibrium and let the system settle into a new equilibrium, taking into account all general equilibrium effects and the mobility of people. Doing so will allow us to simulate the impacts of different trade integration scenarios, taking into account how prices, wages, and the distribution of population across European regions change in response to those shocks.

## 4.1 Numerical procedure for the counterfactuals

Formally, running our counterfactuals entails the following steps:

1. We shock trade costs in different ways. Assume that they change from  $\tau_{rs}$  to  $\tilde{\tau}_{rs}$  (e.g., reducing all NTB's with the U.S. to the intra-EU level). We first eliminate  $\Psi_v$  from (29) by substituting (30) to obtain:

$$\Phi_r^{-k} = \sum_v \frac{\sigma_v \tilde{\tau}_{rv}^{-k}}{\sum_s \sigma_s \left( \frac{\tilde{\tau}_{sv}}{\Phi_s} \right)^{-k}}. \quad (36)$$

Plugging (26) into both sides of (36) yields a system of equations that depends on the labor income shares  $\sigma_r$  only as follows:

$$(\sigma_r^t)^{k+1} \hat{\mu}_r^{\max} (L_r^t)^{-k-1} = \sum_v \frac{\sigma_v^t \tilde{\tau}_{rv}^{-k}}{\sum_s (\sigma_s^t)^{-k} \tilde{\tau}_{sv}^{-k} (\hat{\mu}_s^{\max})^{-1} (L_s^t)^{k+1}}, \quad (37)$$

where superscript  $t$  denotes the current iteration of the system ( $t = 0$  at the beginning of the counterfactual). This system of equations holds exactly — since it has been calibrated in that way — at the initial shares  $\sigma_r^0$  and populations  $L_r^0$ , given initial trade costs  $\tau_{rs}$  and the upper bounds  $\hat{\mu}_r^{\max}$ . However, it no longer holds for the counterfactual trade costs  $\tilde{\tau}_{rs}$ . We hence solve that system for the new income shares  $\sigma_r^{t+1}$  that make it hold with equality. Since the system is not independent, we drop one of the equations and impose the constraint that the income shares sum to one:  $\sum_v \sigma_v = 1$ . The new labor income shares  $\sigma_r^{t+1}$  are those that would prevail after the shock and conditional on the *old* population distribution of the previous iteration  $t$ .

2. Using

$$\Phi_s^{-k} = (\sigma_r^{t+1})^{k+1} \hat{\mu}_r^{\max} (L_r^t)^{-k-1}$$

we solve for the new multilateral resistance terms,  $\hat{\Phi}_s^{t+1}$ , given the initial population distribution at iteration  $t$  and the new income shares at iteration  $t+1$ . Using those terms, we then solve

$$(\hat{\Phi}_s^{t+1})^{-k} = (\sigma_s^{t+1})^{-k} \tilde{\tau}_{ss}^{-k-1} (m_s^d)^{-k-1} (L_s^t)^k$$

for the new cutoffs  $\hat{m}_s^{d,t+1}$ .

3. We construct the new utility

$$\hat{U}_r^{t+1} \propto \frac{1}{\tilde{\tau}_{rr}} \frac{1}{\hat{m}_r^{d,t+1}}$$

associated with the new cutoffs. Given the trade shock, these utility levels will have changed from the initial equilibrium. Hence, the spatial allocation is no longer an equilibrium, i.e., some individuals have incentives to change location in order to take advantage of changes in prices and wages.

4. We hence solve

$$\frac{L_r}{\sum_s L_s} = \frac{\exp(\hat{A}_r + \hat{U}_r^{t+1})}{\sum_s \exp(\hat{A}_s + \hat{U}_s^{t+1})}, \quad (38)$$

for the new population distribution  $L_r^{t+1}$ . Since the system (38) is not independent, we drop one equation and recoup the final population by using the adding-up constraint  $L = \sum_s \hat{L}_s^{t+1}$  at all periods  $t$  (the total population of the system is held constant).

5. We go back to step 1 of the procedure. Since the populations have changed, the income shares need to adjust to solve (37). We solve for the new shares and iterate steps 1–4 of the above procedure until convergence is achieved. Letting  $\mathbf{L}^t$  denote the vector of populations across regions at iteration  $t$  of the algorithm, we define convergence as  $\|\mathbf{L}^{t+1} - \mathbf{L}^t\| \leq \varepsilon$ , i.e., when the change in population between two consecutive iterations becomes sufficiently small.

In Behrens et al. (2017) we prove existence and uniqueness of the initial equilibrium, and we also show that any shock to the system leads (conditional on the initial equilibrium) to a unique counterfactual equilibrium. Hence, our framework is well-suited to investigate the implications of a trade shock on prices, wages, and the regional distribution of population.

## 4.2 Results

We present two series of results. First, we will work at the country level, but we allow for mobility of labor across countries. Second, we will work at the regional level, and allow for labor mobility across both countries and regions.

#### 4.2.1 Countries

Table 2 summarizes our key results from the different counterfactuals that we run. We are especially interested in columns (1) and (5) which summarize the changes in cutoffs and welfare for the different counterfactuals. As we explained before, changes in cutoffs directly map into changes in productivity (since under the Pareto distribution, the inverse of the cutoffs are proportional to the productivity). Table 3 summarizes the counterfactual productivity changes under our different trade integration scenarios.

Three key findings are worth noting from Tables 2 and 3. First, the general pattern is as in our companion paper where we look at the impacts of service and goods trade integration with the US while abstracting from labor mobility. Actually, as can be seen by comparing columns (1) in Table 2 with the same column in the other paper, the effects of integration on cutoffs and productivity are roughly similar in the two approaches, with the effects being marginally stronger if we take into account labor mobility. The reason is that areas that 'gain' attract migrants, which enlarges the local market size and leads to a slight amplification of the productivity gains (see Table 3). Second, we again see that there is a 'core-periphery' pattern as to who loses and who gains. While outsiders to the trade liberalization (e.g., Canada, Australia, Japan, Turkey, Mexico and the other trading partners of the US and EU) experience productivity losses due to the integration, we also have an unequal distribution of gains within the EU. While small countries (Malta, Cyprus) and countries located in the heart of Europe (Austria, Netherlands, Belgium, Germany) are predicted to lose, countries that have less 'central' access to the EU markets are predicted to win (Spain, Portugal, Romania). Note also that Great Britain and France are predicted to win from deeper integration with the US, whereas Ireland (quite surprisingly) might lose. The latter effect is due to Ireland's privileged position with respect to the US, which is likely to erode as barriers of other EU countries with the US fall.

Actually, it is easier to visualize the results graphically using maps. Figures 1 to 3 depict the geographic distribution of productivity changes for service trade liberalization, goods trade liberalization, and both types of liberalization, respectively. Blue indicates a gain while yellow indicates a loss. Deeper blue colors indicate larger gains, and deeper yellow colors indicate larger losses. The geographic pattern we just described is very visible from those figures, with the 'heart of Europe' losing, while the periphery and the Scandinavian countries generally stand to gain. Fig-

Table 2: Counterfactual changes due to the elimination of ‘excess’ trade frictions with the United States (country level).

iso	Country name	(1)		(2)		(3)		(4)		(5)	
		services	goods	services	goods	both	services	goods	both	services	goods
1	AUS	0.362	0.053	0.413	0.362	0.053	0.413	-0.360	-0.053	-0.411	0.000
2	AUT	0.159	0.20	0.179	0.159	0.020	0.179	-0.159	-0.020	-0.178	0.017
3	BEL	0.265	0.033	0.294	0.263	0.033	0.294	-0.262	-0.033	-0.293	0.052
4	BGR	-0.058	-0.012	-0.069	-0.058	-0.012	-0.069	0.058	0.012	0.069	0.058
5	CAN	0.592	0.086	0.675	0.592	0.086	0.675	-0.588	-0.086	-0.670	0.058
6	CHE	0.254	0.031	0.283	0.254	0.031	0.283	-0.253	-0.031	-0.283	-0.137
7	CHL	0.421	0.061	0.480	0.421	0.061	0.480	-0.419	-0.061	-0.478	0.057
8	CYP	-0.168	-0.027	-0.193	-0.168	-0.027	-0.193	0.168	0.027	0.193	-0.419
9	CZE	0.135	0.016	0.150	0.135	0.016	0.150	-0.135	-0.016	-0.135	0.019
10	DEU	0.150	0.016	0.165	0.150	0.016	0.165	-0.150	-0.016	-0.150	0.111
11	DNK	0.071	0.004	0.075	0.071	0.004	0.075	-0.071	-0.004	-0.075	0.026
12	ESP	-0.657	-0.089	-0.738	-0.657	-0.089	-0.738	0.661	0.089	0.743	0.540
13	EST	-0.164	-0.033	-0.195	-0.164	-0.033	-0.195	0.164	0.033	0.196	0.277
14	FIN	-0.164	-0.034	-0.196	-0.164	-0.034	-0.196	0.165	0.034	0.197	0.277
15	FRA	-0.160	0.003	-0.157	-0.160	0.003	-0.157	0.160	-0.003	0.158	0.276
16	GBR	-0.279	-0.037	-0.313	-0.279	-0.037	-0.313	0.279	0.037	0.314	0.338
17	GRC	-0.082	-0.016	-0.097	-0.082	-0.016	-0.097	0.082	0.016	0.097	0.234
18	HRV	0.045	0.002	0.047	0.045	0.002	0.047	-0.045	0.002	-0.046	0.045
19	HUN	0.055	0.004	0.058	0.055	0.004	0.058	-0.055	-0.004	-0.058	0.033
20	IRL	0.152	-0.012	0.139	0.152	-0.012	0.139	-0.152	0.012	-0.139	0.165
21	ISR	0.360	0.052	0.410	0.360	0.052	0.410	-0.358	-0.052	-0.409	0.144
22	ITA	0.044	-0.001	0.042	0.044	-0.001	0.042	-0.044	0.001	-0.044	0.001
23	JPN	0.324	0.047	0.370	0.324	0.047	0.370	-0.323	-0.047	-0.369	0.195
24	KOR	0.321	0.047	0.366	0.321	0.047	0.366	-0.320	-0.047	-0.365	0.167
25	LTU	-0.127	-0.027	-0.153	-0.127	-0.027	-0.153	0.127	0.027	0.153	0.187
26	LVA	-0.158	-0.032	-0.188	-0.158	-0.032	-0.188	0.158	0.032	0.188	0.274
27	MEX	0.549	0.080	0.626	0.549	0.080	0.626	-0.546	-0.080	-0.622	-0.099
28	MLT	-0.080	-0.040	-0.119	-0.080	-0.040	-0.119	0.080	0.040	0.119	0.233
29	NLD	0.208	0.026	0.233	0.208	0.026	0.233	-0.208	-0.026	-0.232	0.081
30	NOR	-0.159	-0.037	-0.193	-0.159	-0.037	-0.193	0.159	0.037	0.194	0.275
31	NZL	0.369	0.054	0.420	0.369	0.054	0.420	-0.367	-0.054	-0.419	0.144
32	POL	0.076	0.007	0.082	0.076	0.007	0.082	-0.076	-0.007	-0.082	0.151
33	PRT	-0.177	-0.045	-0.221	-0.177	-0.045	-0.221	0.177	0.045	0.221	0.284
34	ROM	-0.127	-0.024	-0.150	-0.127	-0.024	-0.150	0.128	0.024	0.150	0.285
35	SVK	0.076	0.007	0.082	0.076	0.007	0.082	-0.076	-0.007	-0.082	0.081
36	SVN	0.139	0.017	0.155	0.139	0.017	0.155	-0.139	-0.017	-0.155	0.136
37	SWE	-0.060	-0.018	-0.078	-0.060	-0.018	-0.078	0.060	0.018	0.068	0.078
38	TUR	0.441	0.065	0.503	0.441	0.065	0.503	-0.439	-0.065	-0.501	-0.047
39	USA	-0.142	-0.021	-0.162	-0.142	-0.021	-0.162	0.143	0.021	0.162	0.266

Notes: Columns 1 to 5 provide for the countries considered in our analysis counterfactual changes in, respectively, cost cutoffs (inversely related to productivity), markups, number of varieties consumed, wages and welfare for each of the 3 counterfactual scenarios we consider: (i) integration in service trade; (ii) integration in goods trade; and (iii) integration for all trade.

Table 3: Counterfactual productivity and population changes (country-level analysis).

	iso	Country	(1)			(2)			(3)		
			TIPP			% change population			Brexit		
			% change productivity	services	goods	both	services	goods	both	services	services
1	AUS	Australia	-0.361	-0.053	-0.411	-0.283	-0.041	-0.322	0.147	0.174	
2	AUT	Austria	-0.159	-0.020	-0.178	-0.116	-0.014	-0.130	0.072	0.083	
3	BEL	Belgium	-0.262	-0.033	-0.293	-0.211	-0.026	-0.236	-0.044	-0.052	
4	BGR	Bulgaria	0.058	0.012	0.069	0.027	0.005	0.031	0.008	0.042	
5	CAN	Canada	-0.588	-0.086	-0.670	-0.442	-0.064	-0.503	0.138	0.173	
6	CHE	Switzerland	-0.253	-0.031	-0.283	-0.330	-0.040	-0.367	0.108	0.077	
7	CHL	Chile	-0.419	-0.061	-0.478	-0.076	-0.011	-0.087	0.040	0.171	
8	CYP	Cyprus	0.168	0.027	0.193	0.092	0.015	0.106	-0.024	-0.059	
9	CZE	Czech Republic	-0.135	-0.016	-0.150	-0.030	-0.003	-0.032	0.024	0.063	
10	DEU	Germany	-0.150	-0.016	-0.165	-0.101	-0.010	-0.110	-0.006	-0.010	
11	DNK	Denmark	-0.071	-0.004	-0.075	-0.050	-0.001	-0.051	-0.020	-0.022	
12	ESP	Spain	0.661	0.089	0.743	0.343	0.047	0.387	-0.003	-0.010	
13	EST	Estonia	0.164	0.033	0.196	0.074	0.014	0.088	0.006	0.013	
14	FIN	Finland	0.164	0.034	0.197	0.145	0.029	0.172	0.020	0.024	
15	FRA	France	0.160	-0.003	0.158	0.133	0.001	0.133	-0.049	-0.070	
16	GBR	Great Britain	0.279	0.036	0.314	0.233	0.031	0.262	-1.120	-1.470	
17	GRC	Greece	0.082	0.016	0.097	0.048	0.009	0.056	0.019	0.047	
18	HRV	Croatia	-0.045	-0.002	-0.046	0.007	0.002	0.010	0.012	0.041	
19	HUN	Hungary	-0.055	-0.004	-0.058	0.004	0.002	0.006	0.015	0.051	
20	IRL	Ireland	-0.152	0.012	-0.139	-0.117	0.013	-0.102	-1.347	-1.522	
21	ISR	Israel	-0.358	-0.053	-0.409	-0.195	-0.028	-0.222	0.117	0.194	
22	ITA	Italy	-0.044	0.001	-0.042	-0.007	0.003	-0.003	0.022	0.036	
23	JPN	Japan	-0.323	-0.047	-0.369	-0.169	-0.025	-0.193	0.093	0.158	
24	KOR	South Korea	-0.320	-0.047	-0.365	-0.132	-0.019	-0.150	0.075	0.157	
25	LTU	Lithuania	0.127	0.027	0.153	0.055	0.011	0.065	0.002	0.001	
26	LVA	Latvia	0.158	0.032	0.189	0.061	0.012	0.073	0.001	-0.003	
27	MEX	Mexico	-0.546	-0.080	-0.622	-0.084	-0.012	-0.095	0.031	0.154	
28	MLT	Malta	0.080	0.040	0.119	0.049	0.018	0.067	-0.034	-0.093	
29	NLD	Netherlands	-0.208	-0.026	-0.232	-0.166	-0.020	-0.184	-0.083	-0.095	
30	NOR	Norway	0.159	0.037	0.194	0.243	0.055	0.295	-0.125	-0.090	
31	NZL	New Zealand	-0.367	-0.054	-0.419	-0.208	-0.030	-0.237	0.107	0.170	
32	POL	Poland	-0.076	-0.007	-0.082	-0.002	0.001	-0.001	0.019	0.067	
33	PRT	Portugal	0.177	0.045	0.221	0.084	0.019	0.103	-0.007	-0.023	
34	ROM	Romania	0.127	0.024	0.150	0.041	0.007	0.048	0.006	0.023	
35	SVK	Slovakia	-0.076	-0.007	-0.082	-0.007	0.001	-0.006	0.020	0.055	
36	SVN	Slovenia	-0.139	-0.017	-0.155	-0.041	-0.004	-0.045	0.031	0.069	
37	SWE	Sweden	0.060	0.018	0.078	0.073	0.019	0.092	-0.013	-0.016	
38	TUR	Turkey	-0.439	-0.065	-0.501	-0.062	-0.009	-0.071	0.044	0.229	
39	USA	United States	0.143	0.021	0.162	0.135	0.020	0.154	0.148	0.179	

Notes: The Table provides counterfactual average productivity and population changes for the countries considered in our analysis stemming from the 4 counterfactual scenarios we consider: i) TIPP between the US and the EU on services trade only; ii) TIPP between the US and the EU on goods trade only; iii) TIPP between the US and the EU on both goods and services trade; iv) Exit of the UK from the EU.

ures 4 to 6 depict the associated changes in population, which are also summarized in column (2) of Table 3. As one can see, the geographic pattern is the same than for changes in productivity: regions that loose productivity quite naturally loose population, and this reinforces slightly the productivity loss.

Last, the gains from service liberalization are a magnitude larger than the gains from goods liberalization. This is expected, since service trade between the US and the EU is far less integrated than goods trade. Our results suggest that there is a strong rationale for focusing on deeper service-trade integration, whereas there is little to be gained from further goods market integration (at least when integration is bringing the level of trade frictions to the one currently prevailing within the EU).

Figure 1: Productivity changes, service trade liberalization with the us (country-level analysis).

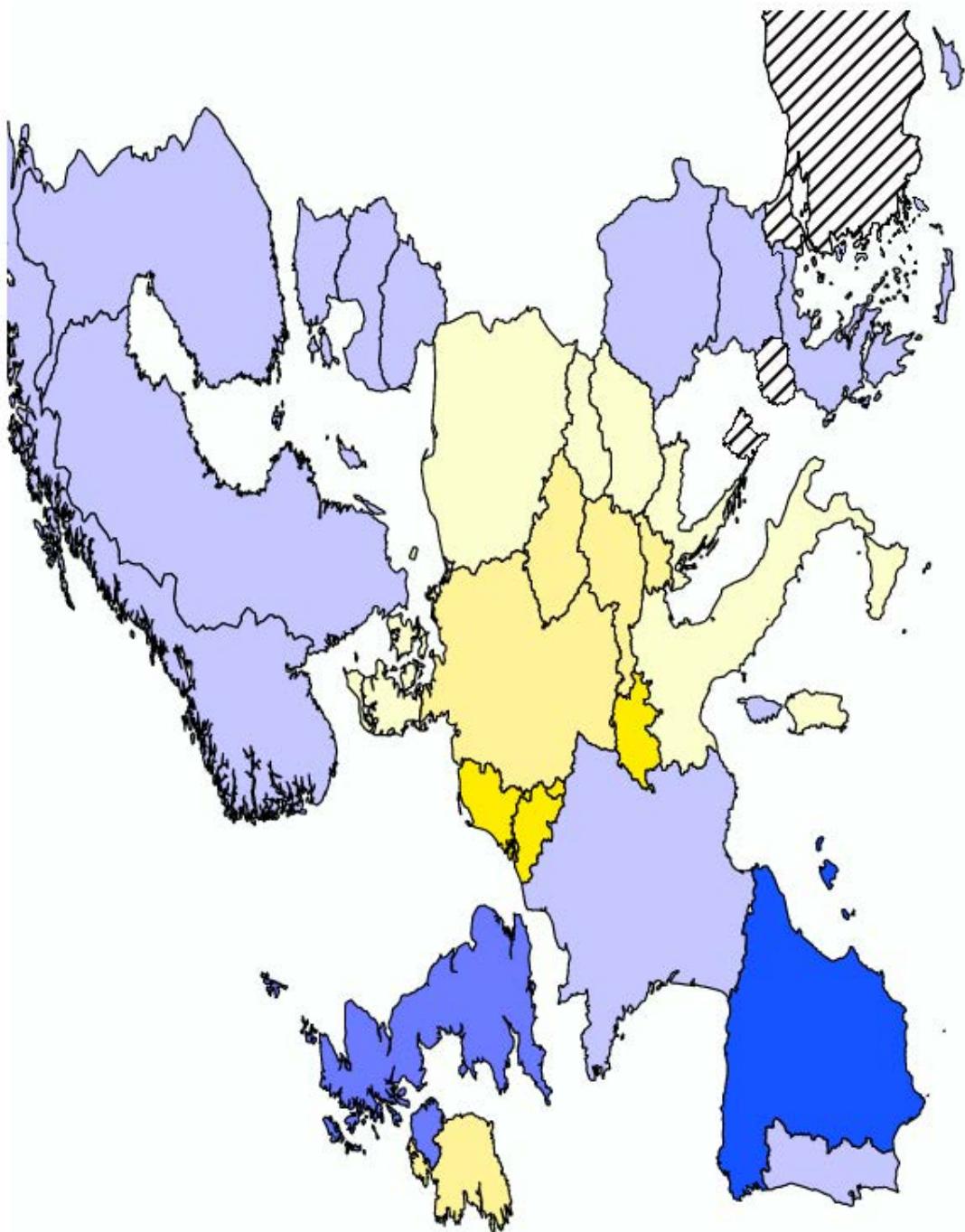


Figure 2: Productivity changes, goods trade liberalization with the us (country-level analysis).

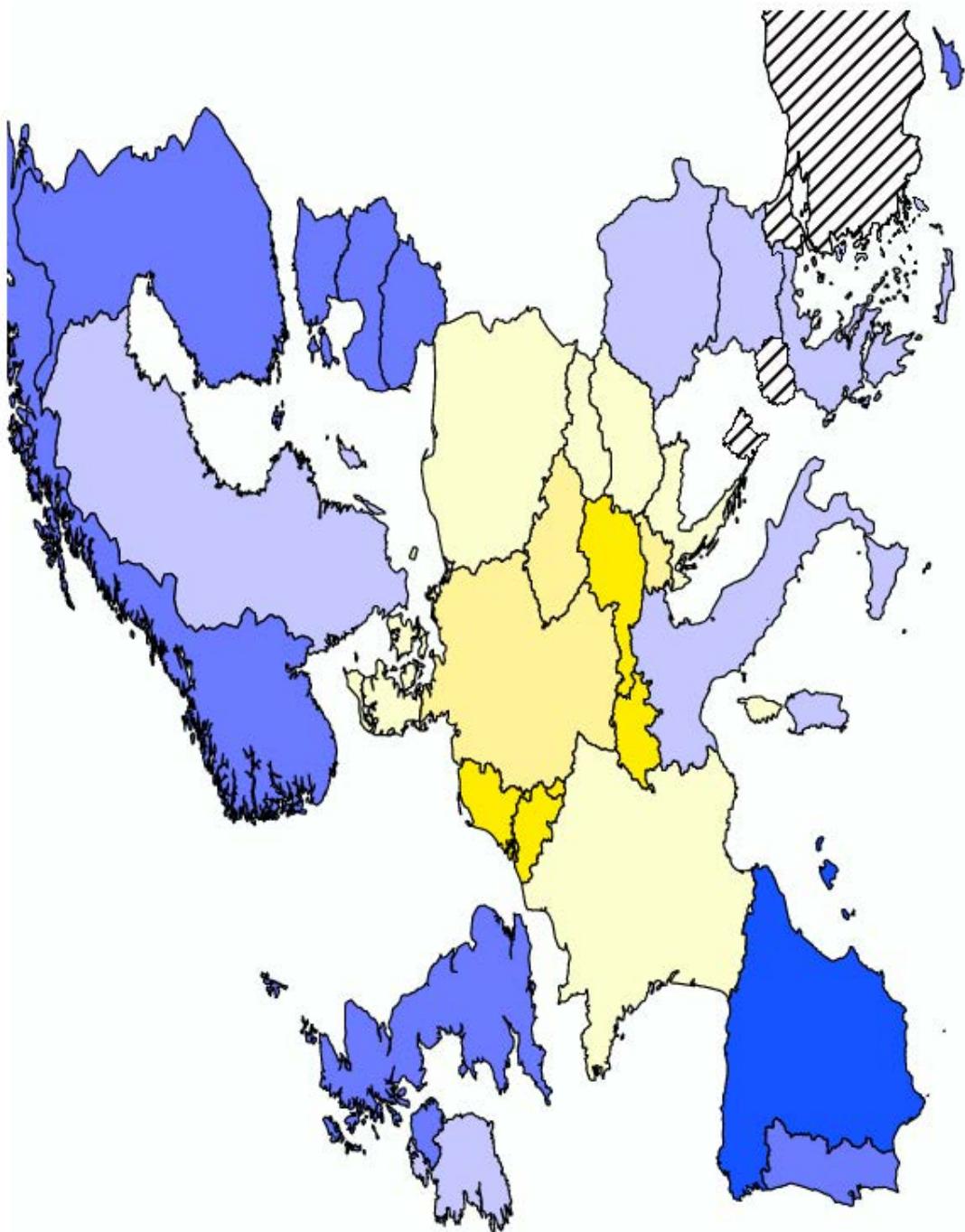


Figure 3: Productivity changes, service and goods trade liberalization with the us (country-level analysis).

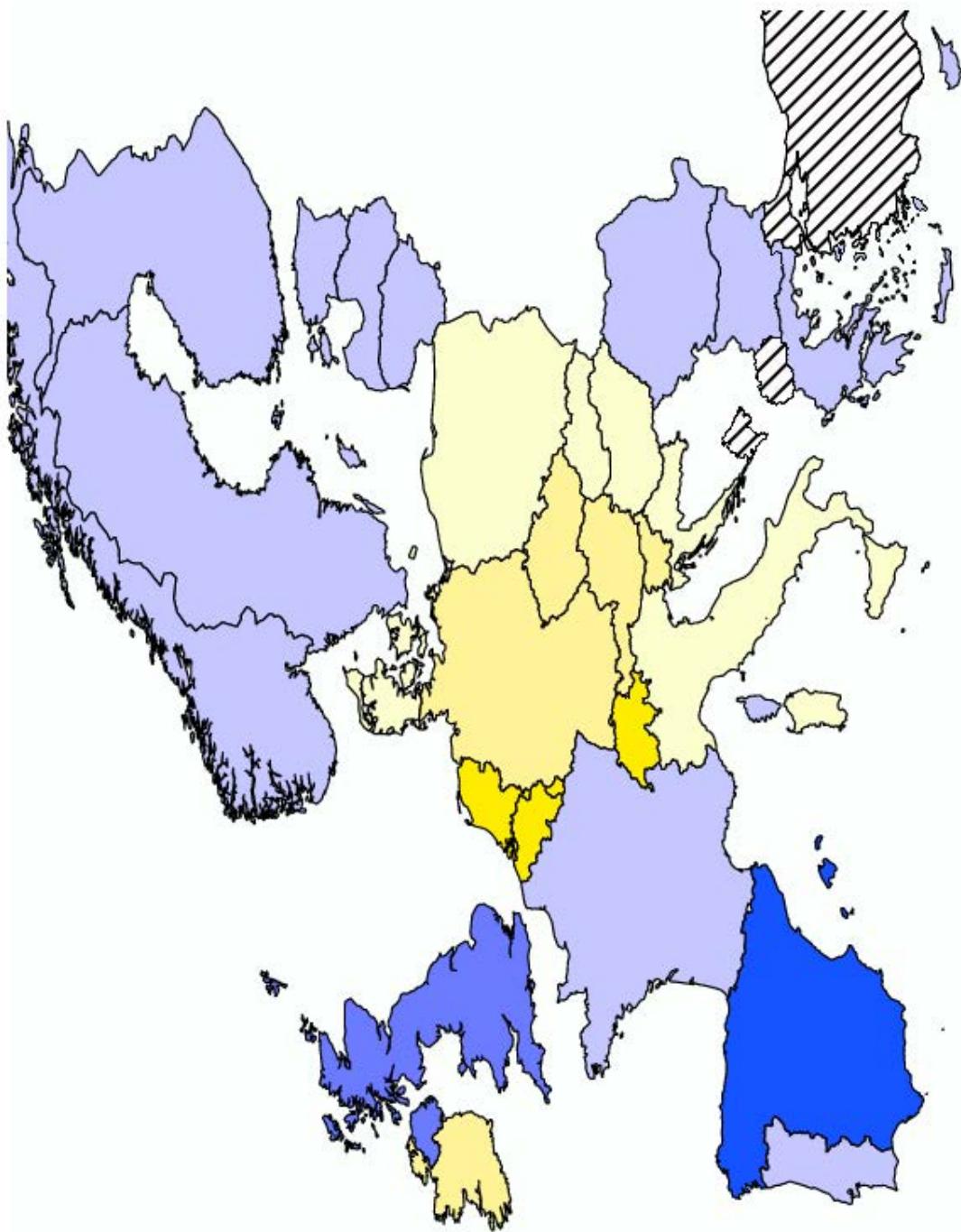


Figure 4: Population changes, service trade liberalization with the us (country-level analysis).

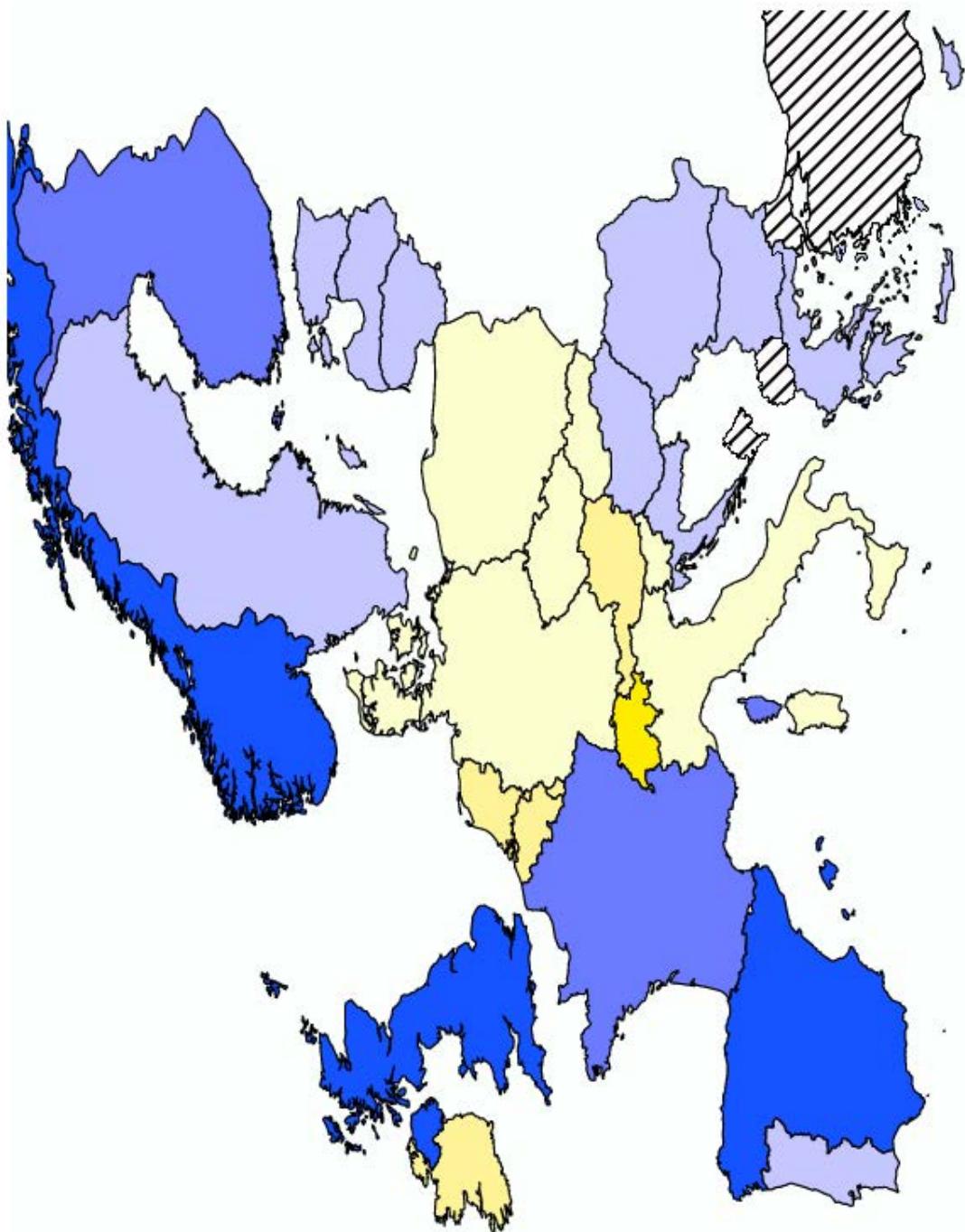


Figure 5: Population changes, goods trade liberalization with the us (country-level analysis).

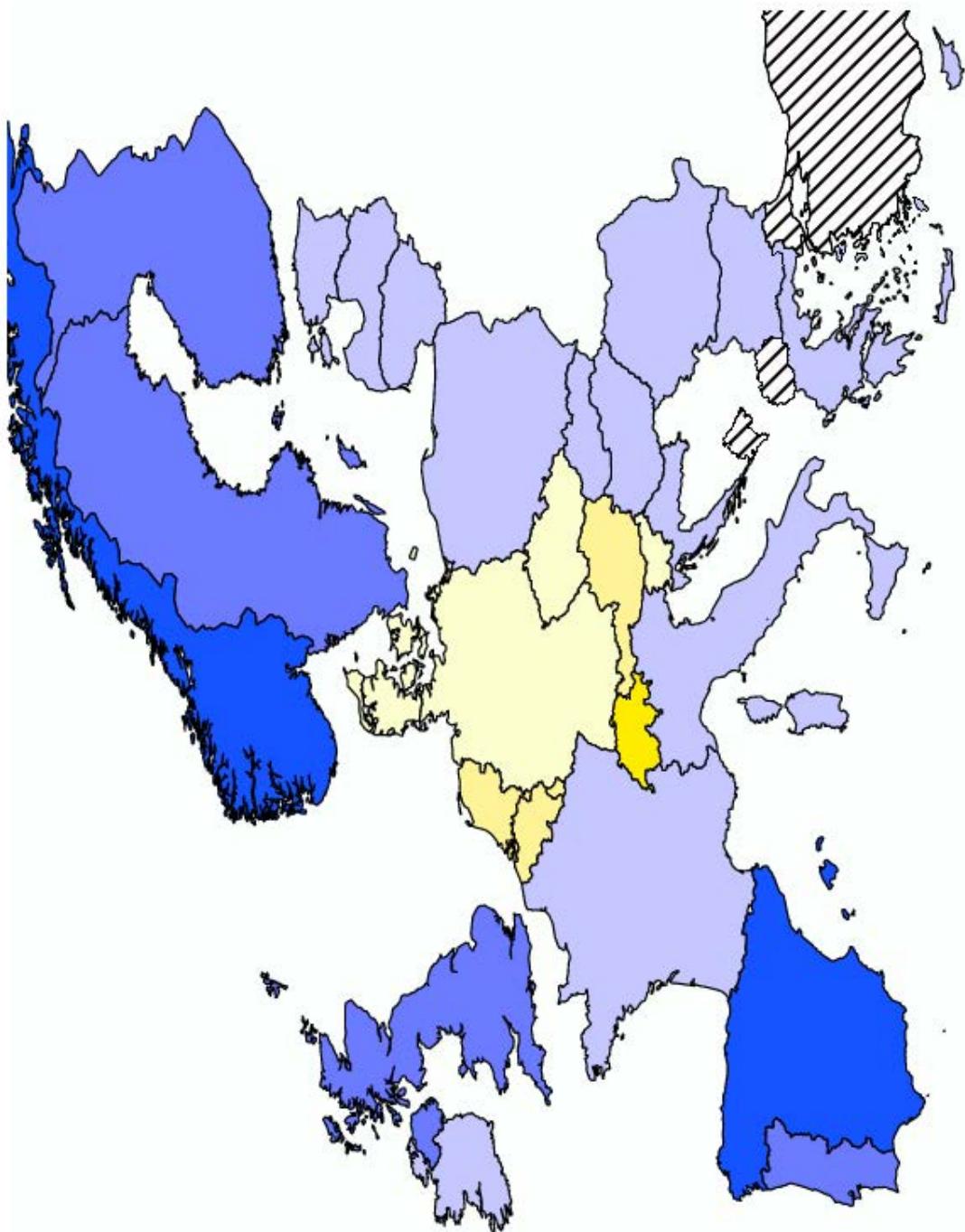
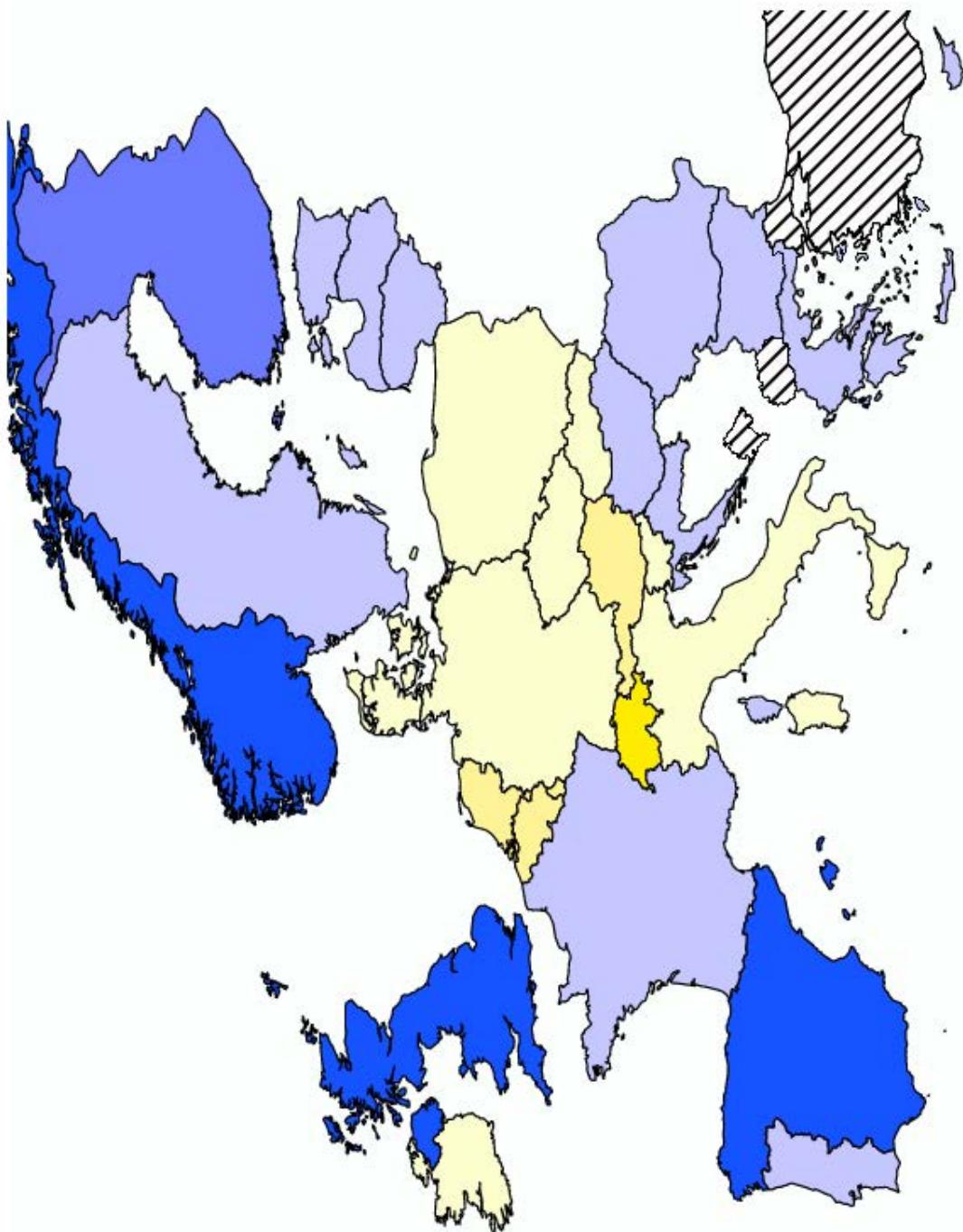


Figure 6: Population changes, service and goods trade liberalization with the us (country-level analysis).



**Brexit.** We now simulate the exit of the UK from the European Union (Brexit). Figures 7 and 8 depict our results for the case of productivity and population changes, respectively. The two big losers from Brexit are the UK and Ireland, who see their productivity fall by 1.47% and 1.52%, respectively. The corresponding population losses are 1.12% for the UK and 1.35% for Ireland. The largest winner in the EU is Switzerland, whose productivity increases by 0.11% and who experiences population growth of 0.078%. A full set of results for all countries is provided in column (3) of Table 3.

Figure 7: Productivity changes, service trade in the wake of Brexit (country-level analysis).

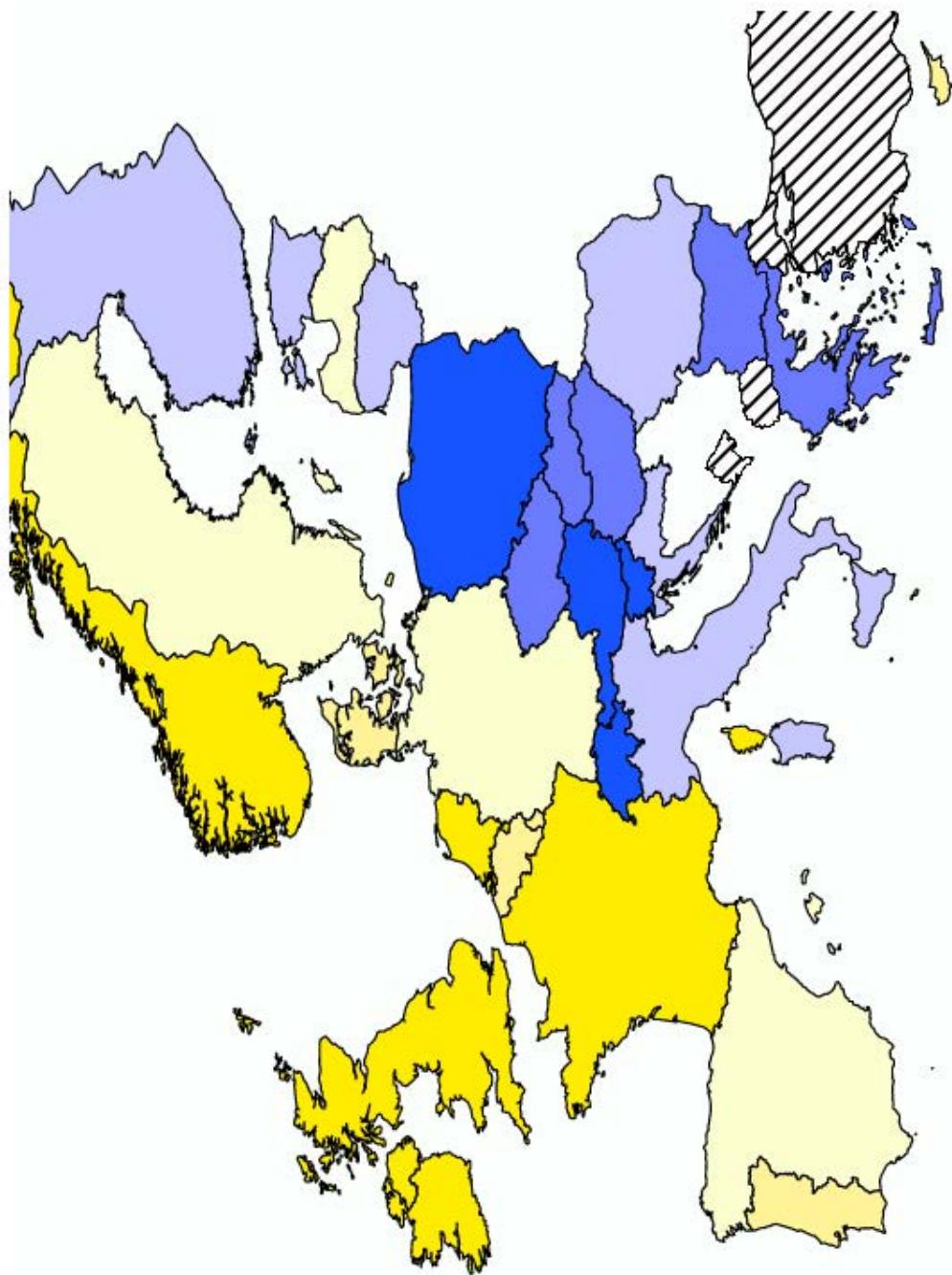
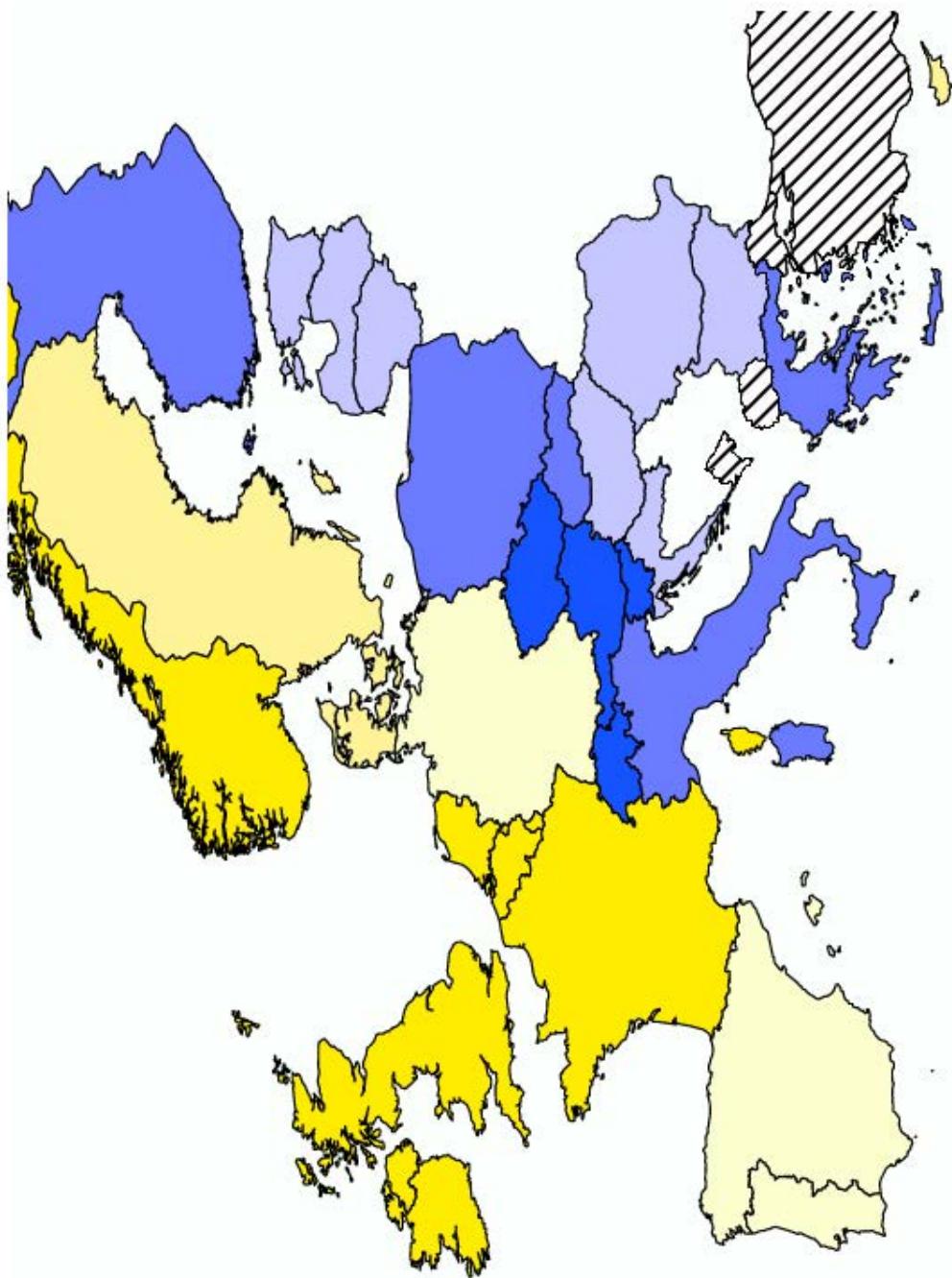


Figure 8: Population changes, service trade in the wake of Brexit (country-level analysis).



#### 4.2.2 Regions

While Table 3 summarizes our key results from the different counterfactuals that we run at the country level, that table masks a substantial amount of within-country heterogeneity. Regions within countries are asymmetrically exposed to trade integration, depending on their geographic position, size, and the country they belong to. We hence now present results for the counterfactual trade liberalization in goods and services (or both) with the US, by breaking down the EU countries into their NUTS2 regions. Together with the rest-of-the-world countries we hence run the model for 286 regions in total (276 NUTS2 regions, and 10 other OECD trading partners).

Figures 9 to 11 visually depict the regional productivity changes due to deeper trade integration, for services, for goods, and for both, respectively. Figures 12 to 14 visually depict the same information for regional population changes. As can be seen, the national ‘core-periphery’ pattern of the productivity and population changes persists, though there are some exceptions. First, large city-regions (Paris, London) tend to loose from deeper service trade integration. The reason is that their large size confer them an advantage that is larger the harder it is to trade. In other words, local size matters the most when trade is quite costly. In that respect, liberalizing service trade is likely to hurt the large city regions by making their local market size less relevant. Second, Ireland actually gains from service trade liberalization when considered at the regional level, whereas it loses when considered at the national level.

Figure 15 depicts the distributions of regional productivity (top panel) and population (bottom panel) changes in the case of service trade liberalization. The simple (unweighted) average productivity change across regions is 0.134%, with standard deviation of 0.26. The region that loses the most is Brussels with -0.24%, whereas the region that gains the most is Highlands and Islands (UK) with 1.02%.

Figure 16 depicts the distributions of regional productivity (top panel) and population (bottom panel) changes in the case of goods trade liberalization. The simple (unweighted) average productivity change across regions is 0.019%, with standard deviation of 0.038. The region that loses the most is Brussels with -0.08%, whereas the region that gains the most is Highlands and Islands (UK) with 0.14%. Note that there is sizable between and within country variation in the distribution of productivity changes. We have an overall variance of 0.261, with a between EU countries

Figure 9: Productivity changes, service trade liberalization with the us (region-level analysis).

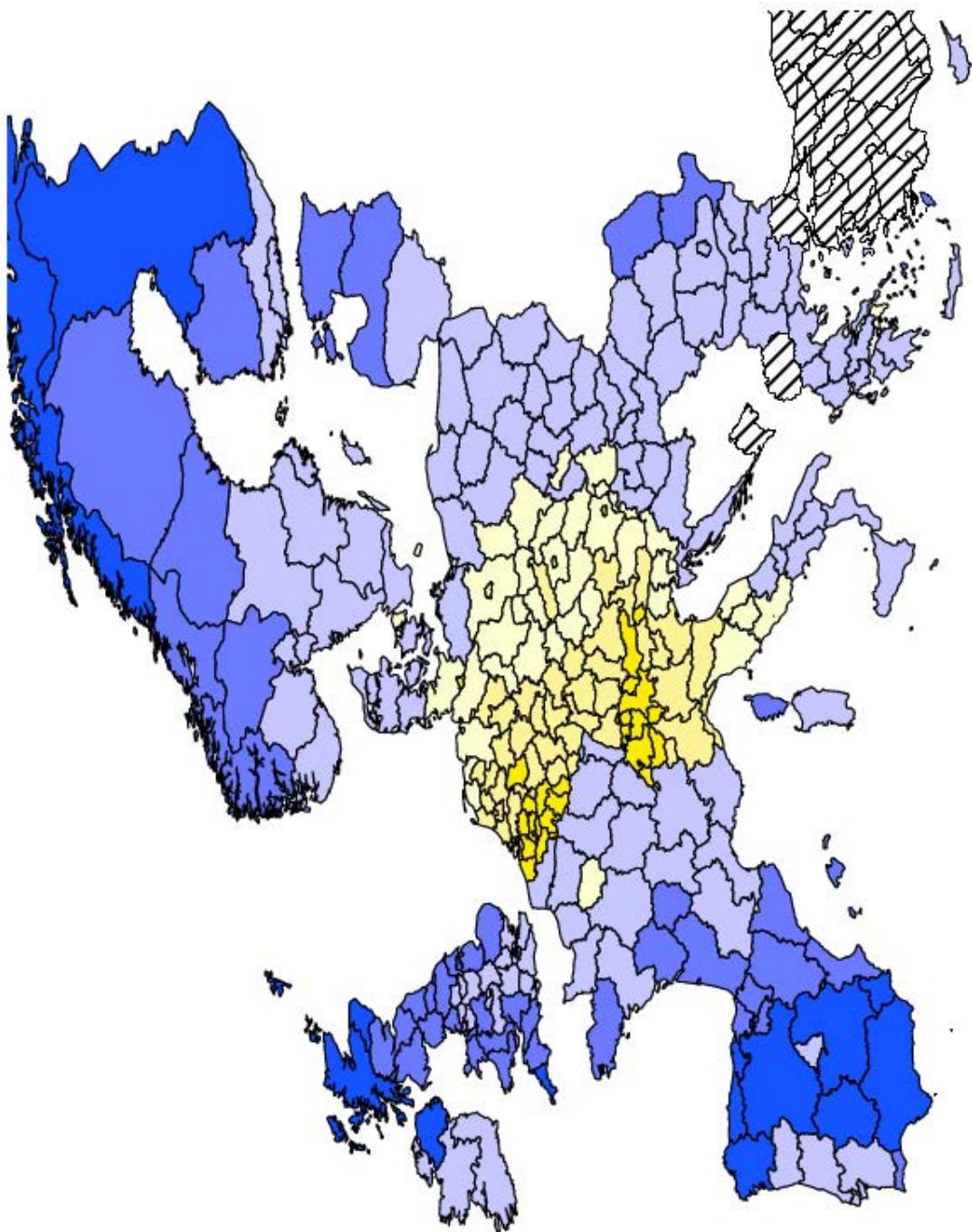


Figure 10: Productivity changes, goods trade liberalization with the us (region-level analysis).

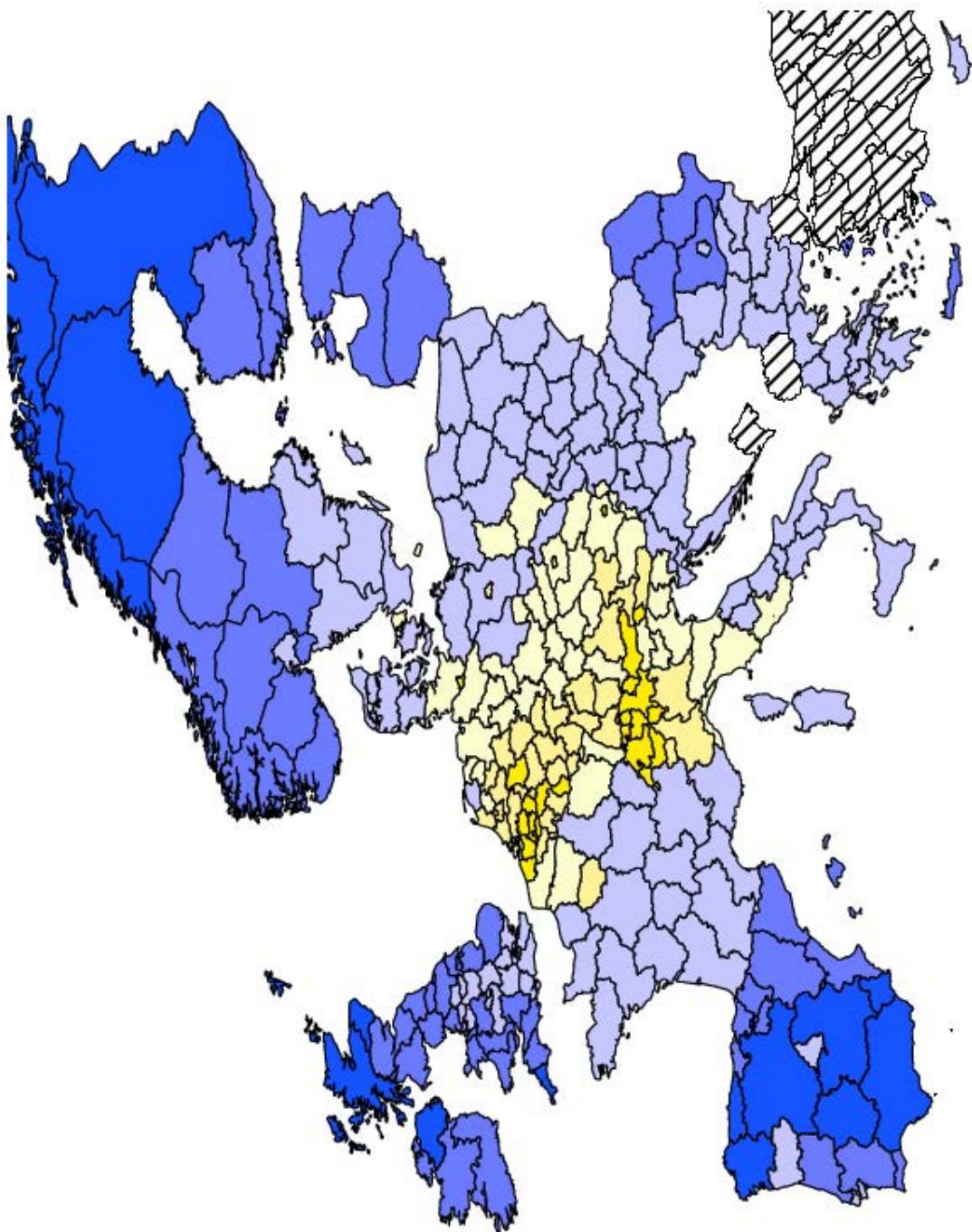


Figure 11: Productivity changes, service and goods trade liberalization with the us (region-level analysis).

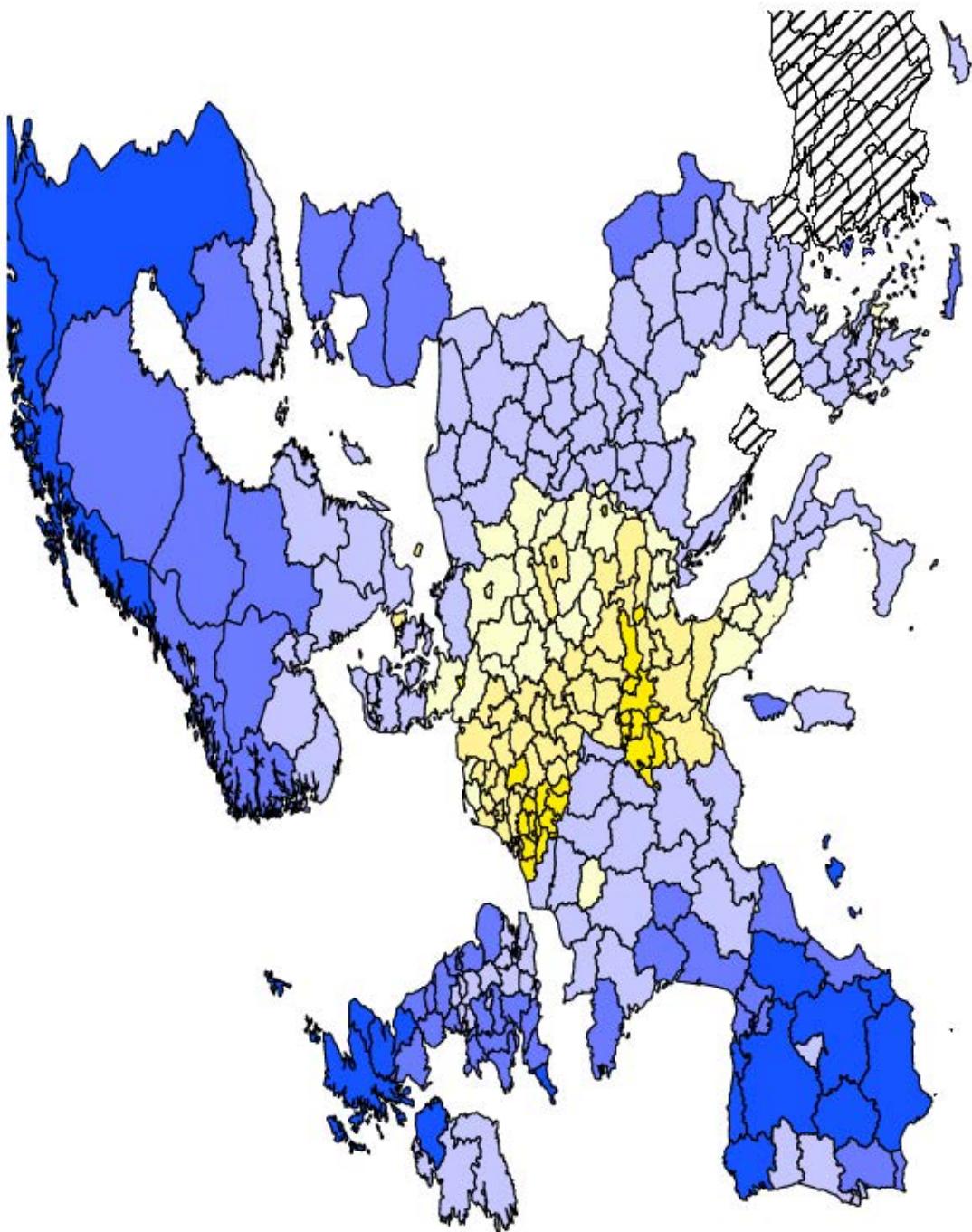


Figure 12: Population changes, service trade liberalization with the us (region-level analysis).

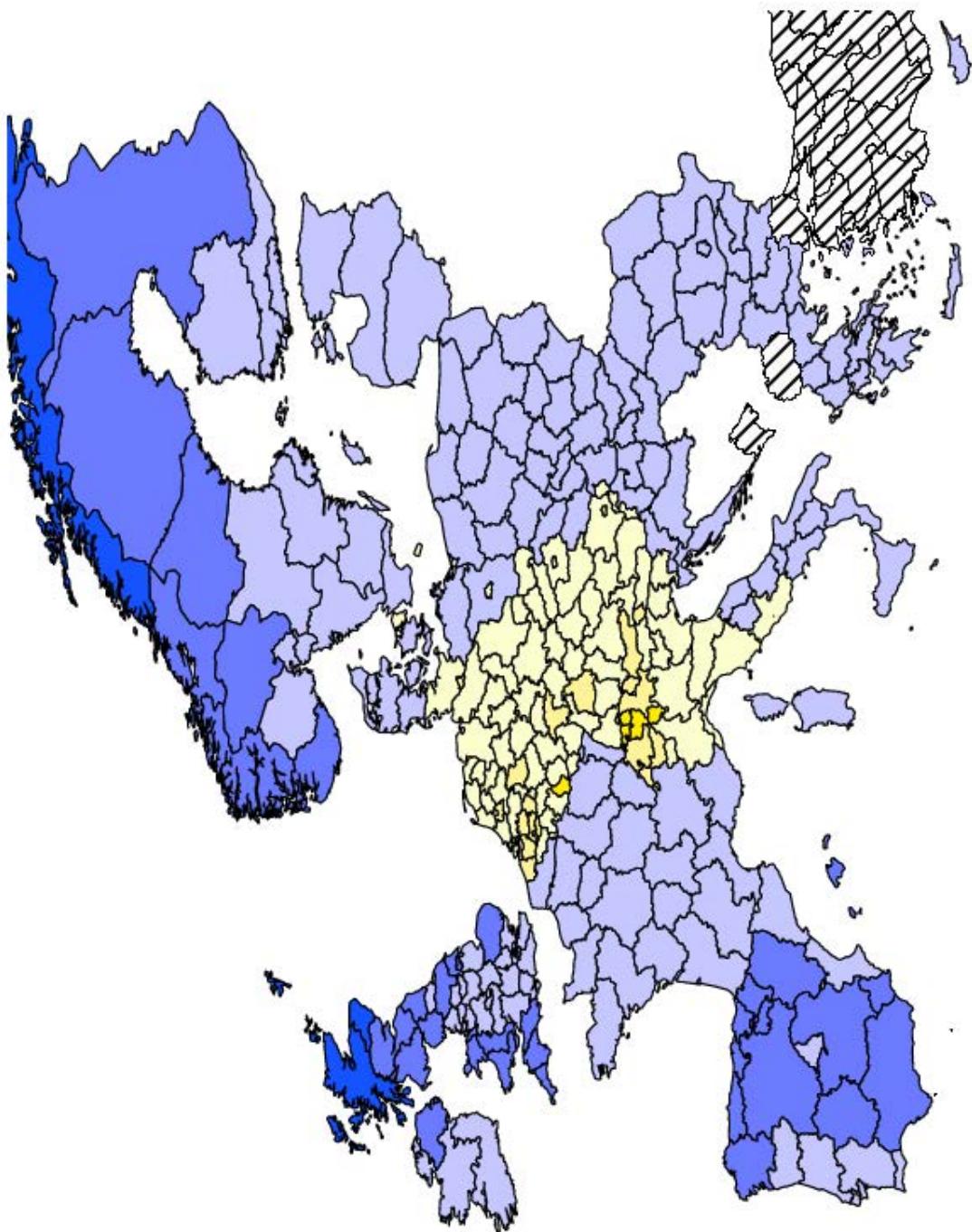


Figure 13: Population changes, goods trade liberalization with the us (region-level analysis).

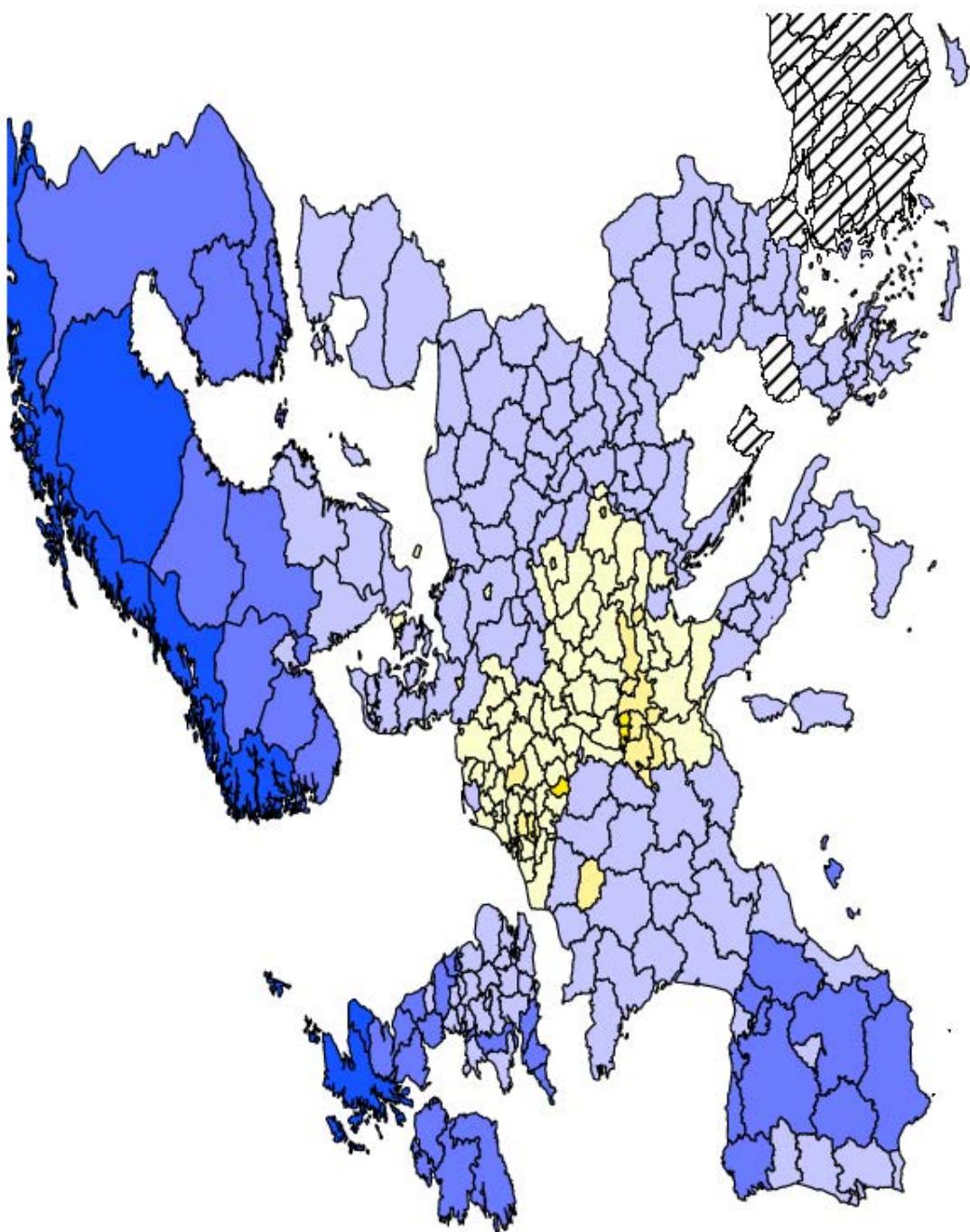


Figure 14: Population changes, service and goods trade liberalization with the us (region-level analysis).

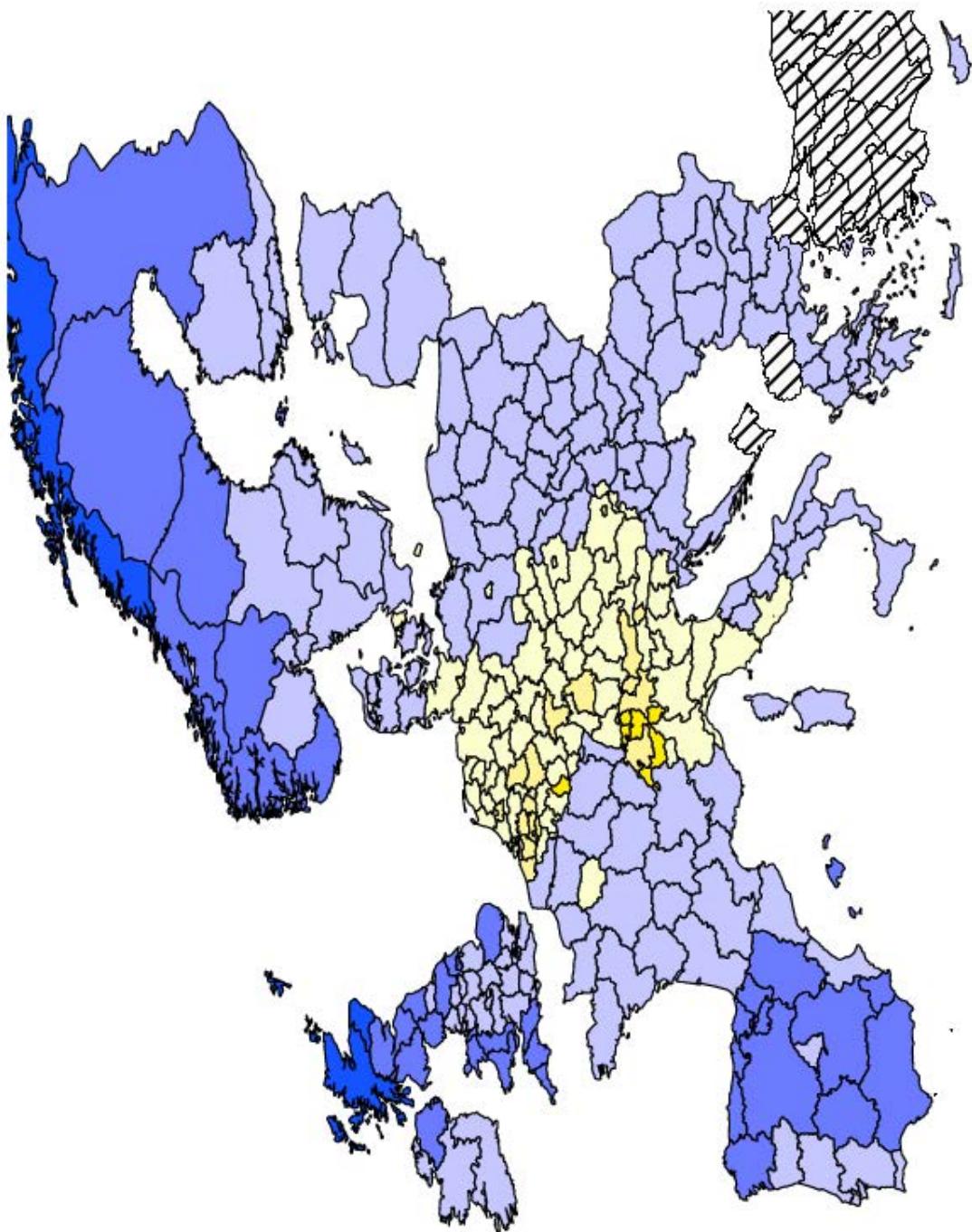


Figure 15: Distribution of productivity and population changes, service trade liberalization.

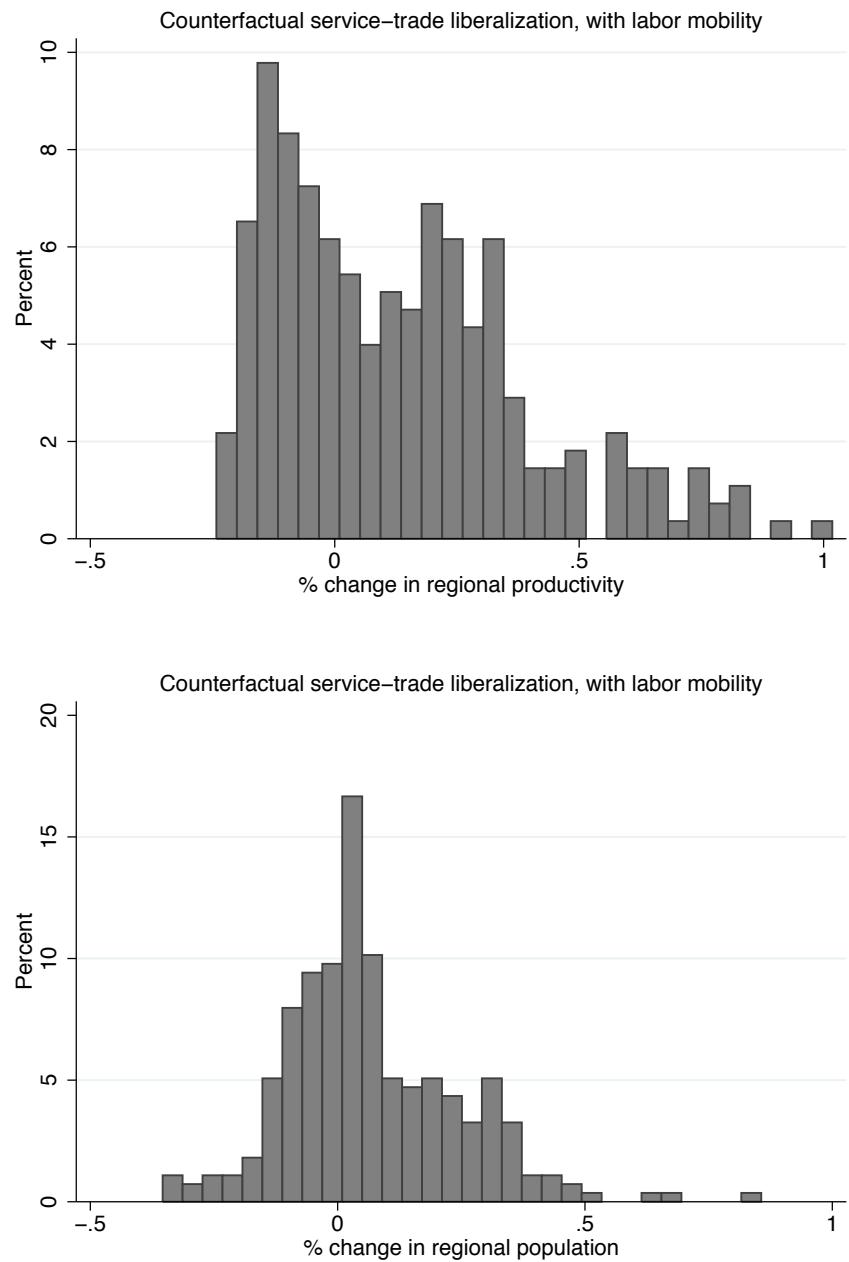
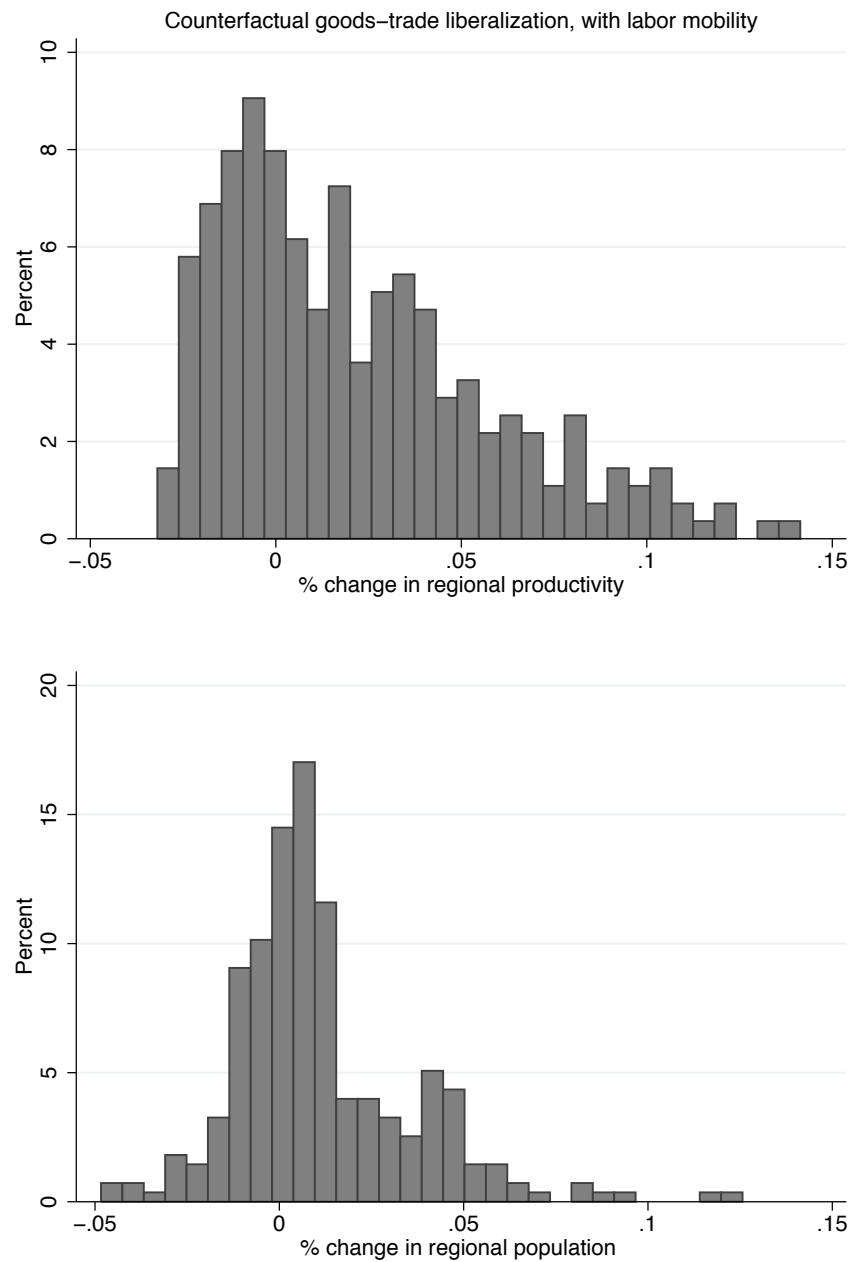


Figure 16: Distribution of productivity and population changes, goods trade liberalization.



component of 0.214, and a within EU countries component of 0.119.

Comparing Figures 15 and 16 reveals that service trade liberalization has effects that are an order of magnitude larger. The reason is that goods trade is already fairly liberalized, whereas service trade is still subject to substantial NTBs. Removing those non-tariff barriers can potentially lead to substantial productivity gains.

**Brexit.** We now simulate the exit of the UK from the European Union (Brexit). The results are summarized in Figure 17 for productivity changes, and in Figure 18 for population changes. As can be seen, regions in the UK and Ireland loose the most in terms of productivity. However, the larger cities are hit less hard, especially London. As can be seen from Figure 18, London, Madrid, or Lisbon gain in terms of population, whereas the remaining regions in those countries loose. Hence, the changes induced by Brexit are likely to favor the larger city regions at the expense of smaller regions.

Figure 17: Productivity changes, service trade in the wake of Brexit (region-level analysis).

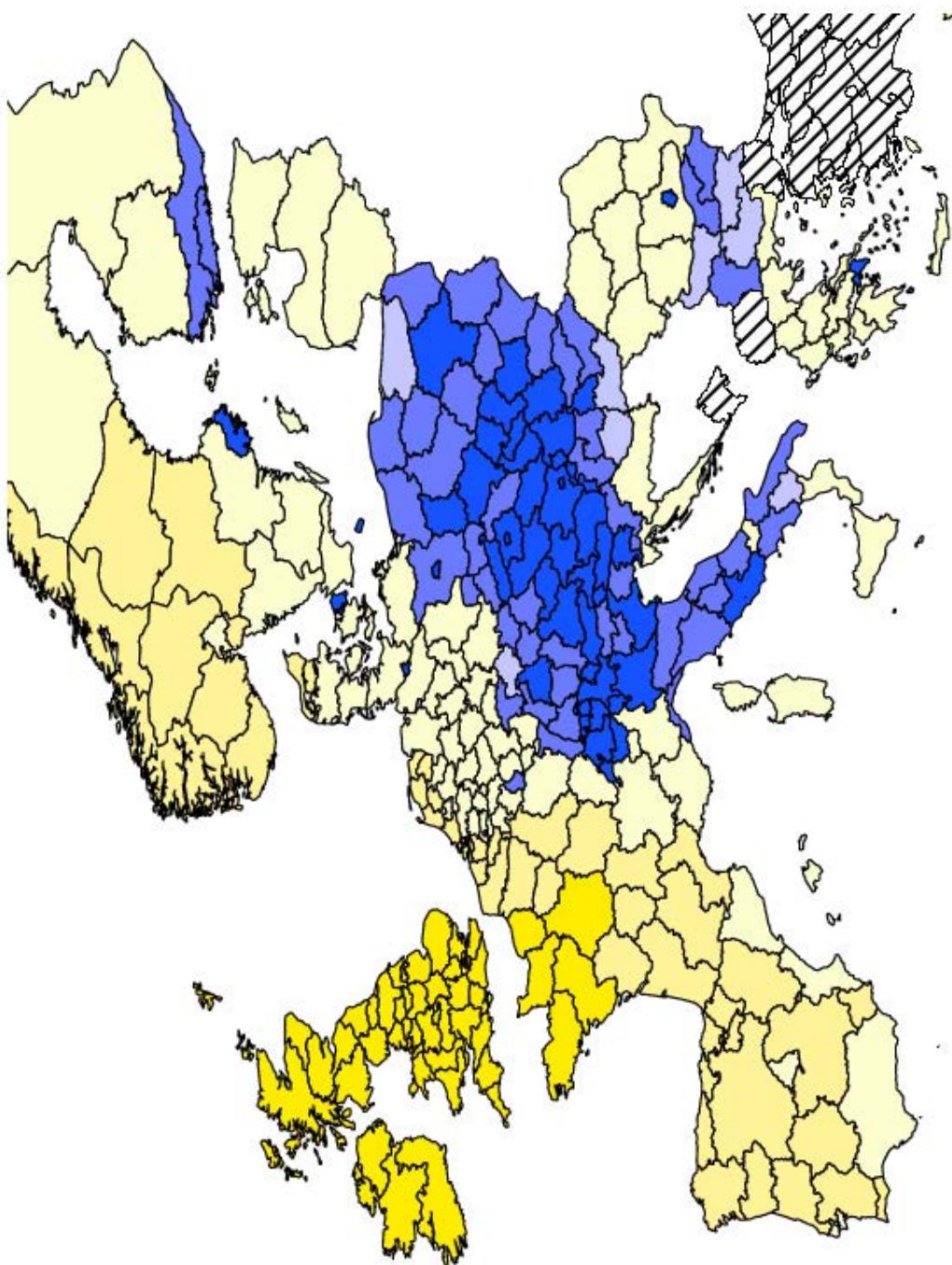
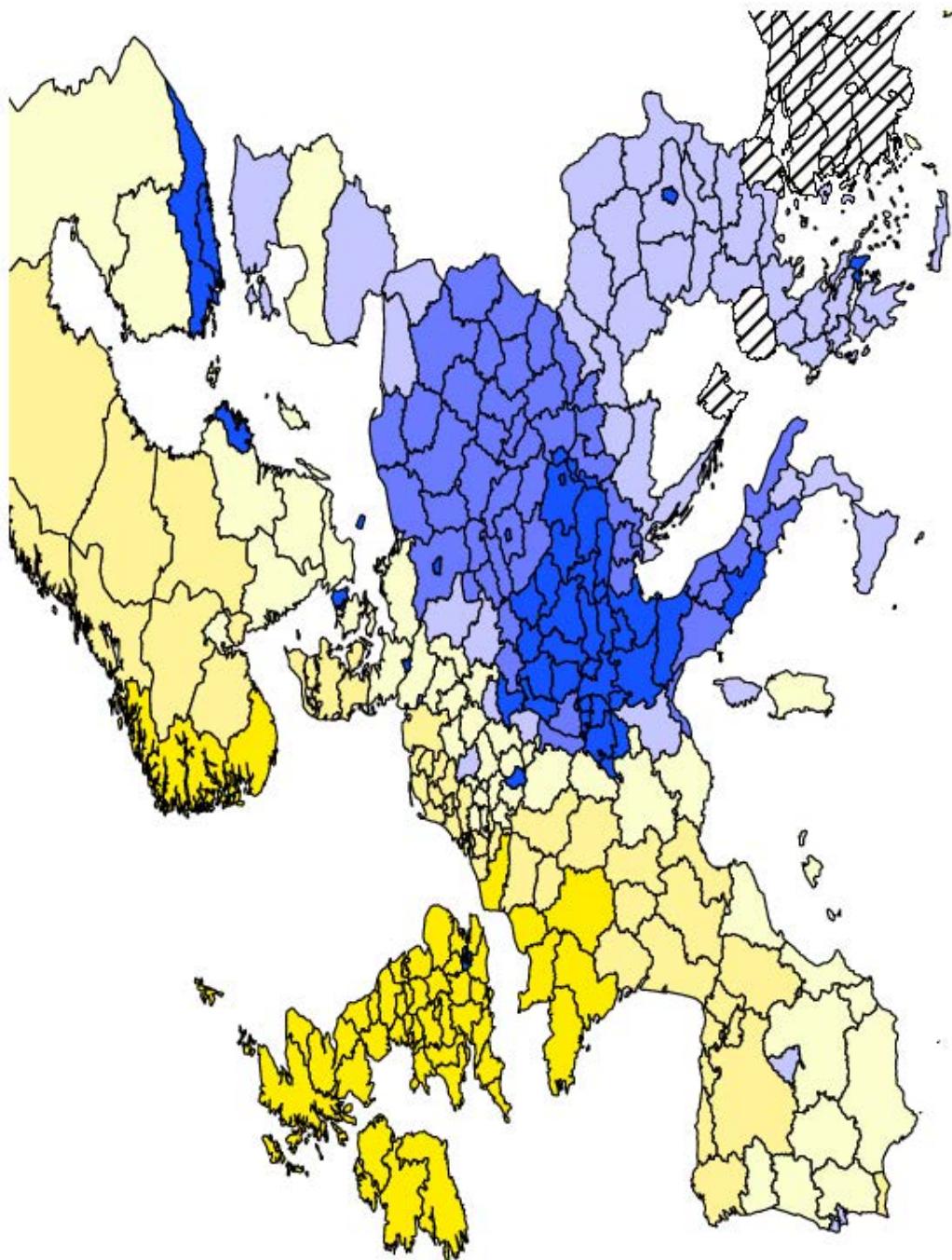


Figure 18: Population changes, service trade in the wake of Brexit (region-level analysis).



## 5 Conclusions

In this paper we provide insights into the impact of NTMs on aggregate country and regional productivity as well as on population movements. More specifically, we first develop a model, drawing upon Behrens et al. (2014) and Behrens et al. (2017), characterized by costly trade, love of variety, heterogeneous firms, labour mobility as well as endogenous markups and productivity. We subsequently quantify the model using goods and services trade data as well as GDP and population for European Economic Area (EEA) regions/countries plus other OECD countries: Australia, Canada, Chile, Israel, Japan, Korea, Mexico, New Zealand, Turkey and the US. In the first part of our analysis we quantify our model and do counterfactual analysis at the country-level for both EEA and non-EEA countries. In the second part of our analysis, we break down EEA countries into the corresponding NUTS-2 regions. We finally assess the importance of NTMs for productivity, markups, population and wages by performing a series of counterfactual experiments. More specifically, we evaluate the impact of implementing the Transatlantic Trade and Investment Partnership (TTIP) between the EEA and the US.

We separately consider a liberalization of trade in goods and a liberalization of trade in services (as well as a joint liberalization) with the latter being a much cleaner instance in which NTMs represent the main existing obstacle to international trade. We find that a liberalization of trade in services will have stronger impacts than a liberalization of trade in goods on EEA countries' productivity. However, gains (and losses) remain modest and in most cases below 1%. Interestingly, countries in the core of the EEA (Germany, Belgium, the Netherlands, etc.) will mainly loose from TTIP while peripheral countries will gain. At the same time, large city-regions (Paris, London) tend to gain less/lose more from deeper service trade integration. The reason is that their large size confer them an advantage that is larger the harder it is to trade. As for population changes, they roughly mirror the pattern of productivity changes and are overall modest. We also perform an additional counterfactual to further isolate the role of NTMs: the exit of the UK from the EEA (Brexit). When focusing on trade in services, we find in this scenario sizeable losses for many EEA countries and in particular for the UK and Ireland (about -1.5% productivity each and with a decrease in population of respectively 1.12% and 1.35%). Furthermore, our results suggest changes induced by Brexit are likely to favor the larger city regions at the expense of smaller regions.

Two key considerations stem from our analysis. First, our findings suggest TTIP would not be beneficial to all EEA countries. As a matter of fact, many core EU countries are expected to lose from the implementation of this agreement. At the same time, gains and losses would be very unevenly distributed across regions within a country depending on size, competitiveness and location. This calls for a careful cost-benefit analysis at the EU/EEA level. Second, the seemingly unavoidable Brexit will bring about losses for many EEA countries (UK and Ireland would lose 1.5% aggregate productivity and more than 1% of their population) while actually benefiting the rest of the world (US included). We believe these figures call for constructive trade negotiations between the EU and the UK in view of what appear to be substantial mutual benefits.

## References

- [1] Anderson, James E., and Eric van Wincoop. 2003. "Gravity with Gravitas: A Solution to the Border Puzzle." *American Economic Review* 93(1): 170–192.
- [2] Behrens, Kristian, Giordano Mion, Yasusada Murata, and Jens Suedekum. 2014. "Trade, Wages, and Productivity." *International Economic Review* 55(4): 1305–1348.
- [3] Behrens, Kristian, Giordano Mion, Yasusada Murata, and Jens Suedekum. 2017. "Spatial Frictions." *Journal of Urban Economics* 97: 40–70.
- [4] Broda, Christian, and David E. Weinstein. 2006. "Globalization and the Gains from Variety." *Quarterly Journal of Economics* 121(2): 541–585.
- [5] De Loecker, Jan. 2011. "Product differentiation, multiproduct firms, and estimating the impact of trade liberalization on productivity." *Econometrica* 79(5): 1407–1451.
- [6] De Loecker, Jan, Pinelopi K. Goldberg, Amit K. Khandelwal, and Nina Pavcnik. 2016. "Prices, markups and trade reform." *Econometrica* 84(2): pp. 445–510.
- [7] Bernard, Andrew B., J. Bradford Jensen, Stephen J. Redding, and Peter K. Schott. 2007. "Firms in international trade." *Journal of Economic Perspectives* 21(3): 105–130.

- [8] Faini, Riccardo. 1999. "European migrants: an endangered species?" In: *Market integration, regionalism and the global economy*. Cambridge University Press, Cambridge, pp. 228–251.
- [9] Faini, Riccardo, Giampaolo Galli, and Pietro Gennari. 1997. "An empirical puzzle: falling migration and growing unemployment differentials among Italian regions." *European Economic Review* 41(3): 571–579.
- [10] Feenstra, Robert C., and David E. Weinstein. 2017. "GLOBALIZATION, MARKUPS AND U.S. WELFARE". *Review of Economic Studies*, forthcoming.
- [11] Gaubert, Cecile. 2015. "Firm sorting and agglomeration." Mimeo, University of California, Berkeley.
- [12] Haskel, Jonathan, and Holger Wolf. 2001. "The Law of One Price—A Case Study." *Scandinavian Journal of Economics* 103(4): 545–558.
- [13] Helpman, Elhanan, Marc J. Melitz, and Yolanda Rubinstein. 2008. "Estimating Trade Flows: Trading Partners and Trading Volumes." *Quarterly Journal of Economics* 123(2): 441–487.
- [14] McFadden, Daniel. 1974. "Conditional Logit Analysis of Qualitative Choice Behavior." In: Zarembka, P. (Ed.), *Frontiers in Econometrics*. Academic Press, New York, pp. 105–142.
- [15] Melitz, Marc J. 2003. "The Impact of Trade on Intra-Industry Reallocations and Aggregate Industry Productivity." *Econometrica* 71(6): 1695–1725.
- [16] Melitz, Marc J., and Gianmarco I. P. Ottaviano. 2008. "Market Size, Trade, and Productivity." *Review of Economic Studies* 75(1): 295–316.
- [17] Murata, Yasusada. 2003. "Product diversity, taste heterogeneity, and geographic distribution of economic activities: market vs. non-market interactions." *Journal of Urban Economics* 53(1): 126–144.
- [18] Simonovska, Ina. 2015. "Income differences and prices of tradables: Insights from an online retailer." *Review of Economic Studies* 82(4): 1612–1656.

- [19] Tabuchi, Takatoshi, and Jacques-François Thisse. 2002. "Taste heterogeneity, labor mobility and economic geography." *Journal of Development Economics* 69(1): 155–177.
- [20] Wolf, Holger C. 2000. "Intranational home bias in trade." *Review of Economics and Statistics* 82(4): 555–563.
- [21] World Bank. 2016. *Doing Business 2016. Measuring Regulatory Quality and Efficiency*. International Bank for Reconstruction and Development / The World Bank: Washington, DC.

# Appendix

## Appendix A: Computational details

### A.1. Derivation of the demand functions.

In this appendix, we derive expression (2). Let  $\lambda$  denote the Lagrange multiplier. The first-order condition for an interior solution to the maximization problem (1) satisfies

$$\alpha e^{-\alpha q_{sr}(i)} = \lambda p_{sr}(i), \quad \forall i \in \Omega_{sr} \quad (\text{A-1})$$

and the budget constraint  $\sum_s \int_{\Omega_{sr}} p_{sr}(k) q_{sr}(k) dk = E_r$ . Taking the ratio of (A-1) for  $i \in \Omega_{sr}$  and  $j \in \Omega_{vr}$  yields

$$q_{sr}(i) = q_{vr}(j) + \frac{1}{\alpha} \ln \left[ \frac{p_{vr}(j)}{p_{sr}(i)} \right] \quad \forall i \in \Omega_{sr}, \forall j \in \Omega_{vr}.$$

Multiplying this expression by  $p_{vr}(j)$ , integrating with respect to  $j \in \Omega_{vr}$ , and summing across all origin regions  $v$  we obtain

$$q_{sr}(i) \sum_v \int_{\Omega_{vr}} p_{vr}(j) dj = \underbrace{\sum_v \int_{\Omega_{vr}} p_{vr}(j) q_{vr}(j) dj}_{\equiv E_r} + \frac{1}{\alpha} \sum_v \int_{\Omega_{vr}} \ln \left[ \frac{p_{vr}(j)}{p_{sr}(i)} \right] p_{vr}(j) dj. \quad (\text{A-2})$$

Using  $\bar{p}_r \equiv (1/N_r^c) \sum_v \int_{\Omega_{vr}} p_{vr}(j) dj$ , expression (A-2) can be rewritten as follows:

$$\begin{aligned} q_{sr}(i) &= \frac{E_r}{N_r^c \bar{p}_r} - \frac{1}{\alpha} \ln p_{sr}(i) + \frac{1}{\alpha N_r^c \bar{p}_r} \sum_v \int_{\Omega_{vr}} \ln [p_{vr}(j)] p_{vr}(j) dj \\ &= \frac{E_r}{N_r^c \bar{p}_r} - \frac{1}{\alpha} \ln \left[ \frac{p_{sr}(i)}{N_r^c \bar{p}_r} \right] + \frac{1}{\alpha} \sum_v \int_{\Omega_{vr}} \ln \left[ \frac{p_{vr}(j)}{N_r^c \bar{p}_r} \right] \frac{p_{vr}(j)}{N_r^c \bar{p}_r} dj, \end{aligned}$$

which, given the definition of  $h_r$ , yields (2).

### A.2. Derivation of the firm-level variables and properties of $W$

Since firms in country  $r$  differ only by their marginal labor requirements, we can express all firm-level variables in terms of  $m$ . Solving the first-order conditions (6)

for profit maximization, the profit-maximizing prices and quantities, as well as operating profits, are given by:

$$p_{rs}(m) = \frac{\tau_{rs}mw_r}{W}, \quad q_{rs}(m) = \frac{1}{\alpha}(1 - W), \quad \pi_{rs} = \frac{L_s\tau_{rs}mw_r}{\alpha}(W^{-1} + W - 2), \quad (\text{A-3})$$

where  $W$  denotes the Lambert  $W$  function with argument  $em/m_{rs}^x$  that we suppress to alleviate notation (see Corless *et al.*, 1996, for a survey). To derive expressions (A-3) use  $p_s^d = m_{rs}^x\tau_{rs}w_r$  so that the first-order condition (6) can be rewritten as

$$\ln \left[ \frac{m_{rs}^x\tau_{rs}w_r}{p_{rs}(m)} \right] = 1 - \frac{\tau_{rs}mw_r}{p_{rs}(m)}.$$

Taking the exponential of both sides and rearranging terms, we have

$$e \frac{m}{m_{rs}^x} = \frac{\tau_{rs}mw_r}{p_{rs}(m)} e^{\frac{\tau_{rs}mw_r}{p_{rs}(m)}}.$$

Noting that the Lambert  $W$  function is defined as  $\varphi = W(\varphi)e^{W(\varphi)}$  and setting  $\varphi = em/m_{rs}^x$ , we obtain  $W(em/m_{rs}^x) = \tau_{rs}mw_r/p_{rs}(m)$ , which implies  $p_{rs}(m)$  as given in (A-3). The expression for quantities  $q_{rs}(m) = (1/\alpha)[1 - \tau_{rs}mw_r/p_{rs}(m)]$  and the expression for operating profits  $\pi_{rs}(m) = L_s q_{rs}(m) [p_{rs}(m) - \tau_{rs}mw_r]$  are then straightforward to compute.

Turning to the properties of the Lambert  $W$  function,  $\varphi = W(\varphi)e^{W(\varphi)}$  implies that  $W(\varphi) \geq 0$  for all  $\varphi \geq 0$ . Taking logarithms on both sides of the definition of  $W$  and differentiating yields

$$W'(\varphi) = \frac{W(\varphi)}{\varphi[W(\varphi) + 1]} > 0$$

for all  $\varphi > 0$ . Finally, we have  $0 = W(0)e^{W(0)}$ , which implies  $W(0) = 0$ ; and  $e = W(e)e^{W(e)}$ , which implies  $W(e) = 1$ .

Since  $W(0) = 0$ ,  $W(e) = 1$  and  $W' > 0$  for all non-negative arguments, we have  $0 \leq W \leq 1$  if  $0 \leq m \leq m_{rs}^x$ . The expressions in (A-3) show that a firm in  $r$  with a draw  $m_{rs}^x$  (equal to the cutoff labor requirement for selling to market  $s$ ) charges a price equal to marginal cost, faces zero demand, and earns zero operating profits in market  $s$ . Furthermore, it follows that  $\partial p_{rs}(m)/\partial m > 0$ ,  $\partial q_{rs}(m)/\partial m < 0$ , and  $\partial \pi_{rs}(m)/\partial m < 0$ . In words, firms with higher productivity (lower  $m$ ) charge lower prices, sell larger quantities, and earn higher operating profits. These properties are similar to those of the Melitz (2003) model with CES preferences. Yet, our

specification with variable demand elasticity also features higher markups for more productive firms (see, e.g., de Loecker, 2011; de Locker et al., 2016). Indeed, the *origin-destination markup* for a firm located in country  $r$  and selling to country  $s$  is given by

$$\Lambda_{rs}(m) \equiv \frac{p_{rs}(m)}{\tau_{rs} m w_r} = \frac{1}{W}, \quad (\text{A-4})$$

thus implying that  $\partial \Lambda_{rs}(m) / \partial m < 0$ . Melitz and Ottaviano (2008) have a similar effect in their model, yet they use quasi-linear preferences which makes the model not really amenable to counterfactual analysis. We incorporate this feature of markups into a full-fledged general equilibrium model with income effects for varieties that can be taken neatly to the data.

### A.3. Equilibrium conditions using the Lambert $W$ function

In this appendix, we restate the equilibrium conditions (9)–(11) for the multicountry case using the Lambert  $W$  function.

First, plugging (A-3) into (9), zero expected profits can be rewritten as

$$\frac{1}{\alpha} \sum_s L_s \tau_{rs} \int_0^{m_{rs}^x} m \left[ W \left( e \frac{m}{m_{rs}^x} \right)^{-1} + W \left( e \frac{m}{m_{rs}^x} \right) - 2 \right] dG_r(m) = F_r. \quad (\text{A-5})$$

Observe that this condition depends solely on the cutoffs  $m_{rs}^x$  and that it is independent of the mass of entrants. Using (A-3), the labor market clearing condition (10) becomes

$$N_r^E \left\{ \frac{1}{\alpha} \sum_s L_s \tau_{rs} \int_0^{m_{rs}^x} m \left[ 1 - W \left( e \frac{m}{m_{rs}^x} \right) \right] dG_r(m) + F_r \right\} = L_r. \quad (\text{A-6})$$

Finally, using (A-3) the trade balance condition (11) is given by

$$\begin{aligned} & N_r^E w_r \sum_{s \neq r} L_s \tau_{rs} \int_0^{m_{rs}^x} m \left[ W \left( e \frac{m}{m_{rs}^x} \right)^{-1} - 1 \right] dG_r(m) \\ &= L_r \sum_{s \neq r} N_s^E \tau_{sr} w_s \int_0^{m_{sr}^x} m \left[ W \left( e \frac{m}{m_{sr}^x} \right)^{-1} - 1 \right] dG_s(m). \end{aligned} \quad (\text{A-7})$$

We next apply the region-specific Pareto distributions  $G_r(m) = (m/m_r^{\max})^k$  to the system (A-5)–(A-7). We then have a number of integrals that involve the Lambert

$W$  function. To compute closed-form expressions for those integrals, we use the change in variables suggested by Corless *et al.* (1996, p.341). Let

$$z \equiv W\left(e \frac{m}{I}\right), \quad \text{so that} \quad e \frac{m}{I} = ze^z, \quad \text{where} \quad I \in \{m_r^d, m_{rs}^x\},$$

where we drop the subscript  $r$  to alleviate notation. The change in variables then yields  $dm = (1+z)e^{z-1}Idz$ , with the new integration bounds given by 0 and 1. This allows us to rewrite all integrals in simplified form.

**A.3.1.** First, consider the following expression, which appears when integrating firms' outputs:

$$\int_0^I m \left[ 1 - W\left(e \frac{m}{I}\right) \right] dG_r(m) = \kappa_1 (m_r^{\max})^{-k} I^{k+1},$$

where  $\kappa_1 \equiv ke^{-(k+1)} \int_0^1 (1-z^2) (ze^z)^k e^z dz > 0$  is a constant term which solely depends on the shape parameter  $k$ .

**A.3.2.** Second, the following expression appears when integrating firms' operating profits:

$$\int_0^I m \left[ W\left(e \frac{m}{I}\right)^{-1} + W\left(e \frac{m}{I}\right) - 2 \right] dG_r(m) = \kappa_2 (m_r^{\max})^{-k} I^{k+1},$$

where  $\kappa_2 \equiv ke^{-(k+1)} \int_0^1 (1+z) (z^{-1} + z - 2) (ze^z)^k e^z dz > 0$  is a constant term which solely depends on the shape parameter  $k$ .

**A.3.3.** Third, the following expression appears when deriving the (expenditure share) weighted average of markups:

$$\int_0^I m \left[ W\left(e \frac{m}{I}\right)^{-2} - W\left(e \frac{m}{I}\right)^{-1} \right] dG_r(m) = \kappa_3 (m_r^{\max})^{-k} I^{k+1},$$

where  $\kappa_3 \equiv ke^{-(k+1)} \int_0^1 (z^{-2} - z^{-1})(1+z)(ze^z)^k e^z dz > 0$  is a constant term which solely depends on the shape parameter  $k$ .

**A.3.4.** Finally, the following expression appears when integrating firms' revenues:

$$\int_0^I m \left[ W \left( e \frac{m}{I} \right)^{-1} - 1 \right] dG_r(m) = \kappa_4 (m_r^{\max})^{-k} I^{k+1},$$

where  $\kappa_4 \equiv k e^{-(k+1)} \int_0^1 (z^{-1} - z) (z e^z)^k e^z dz > 0$  is a constant term which solely depends on the shape parameter  $k$ . Using the expressions for  $\kappa_1$  and  $\kappa_2$ , one can verify that  $\kappa_4 = \kappa_1 + \kappa_2$ .

Using the expressions (A-5)–(A-7) and the results in **A.3.1–A.3.4** yields, after some more tedious but standard algebra, the expressions (12)–(14) given in the main text.

## A.4. Other equilibrium expressions

In this appendix, we derive additional expressions that are required to characterize the equilibrium and to quantify the consequences of changes in trade costs.

**A.4.1. The mass of varieties consumed.** Using  $N_r^c$  as defined in (8), the export cutoff and the mass of entrants as given by (7) and (15), and making use of the Pareto distribution, we obtain:

$$N_r^c = \frac{\kappa_2}{\kappa_1 + \kappa_2} (m_r^d)^k \sum_s \frac{L_s}{F_s(m_s^{\max})^k} \left( \frac{\tau_{rr} w_r}{\tau_{sr} w_s} \right)^k = \frac{\alpha}{\kappa_1 + \kappa_2} \frac{(m_r^d)^k}{\tau_{rr}} \sum_s L_s \tau_{rr} \left( \frac{\tau_{rr} w_r}{\tau_{sr} w_s} \right)^k \frac{\kappa_2}{\alpha F_s(m_s^{\max})^k}.$$

Using the definition of  $\mu_s^{\max}$ , and noting that the summation in the foregoing expression appears in the equilibrium relationship (16), we can then express the mass of varieties consumed in region  $r$  as given in (17).

**A.4.2 The (expenditure share) weighted average markup.** Plugging (A-3) and (A-4) into the definition (18), the (expenditure share) weighted average markup in the multi-region case can be rewritten as

$$\bar{A}_r^c = \frac{1}{\alpha E_r \sum_s N_s^E G_s(m_{sr}^x)} \sum_s N_s^E \tau_{sr} w_s \int_0^{m_{sr}^x} m \left( W^{-2} - W^{-1} \right) dG_s(m),$$

where the argument  $em/m_{sr}^x$  of the Lambert  $W$  function is suppressed to alleviate notation. As shown in Appendix A.3.3, the integral term in the above expression is given by  $\kappa_3 (m_s^{\max})^{-k} (m_{sr}^x)^{k+1} = \kappa_3 G_s(m_{sr}^x) m_{sr}^x$ . Using this together with (7) and  $E_r = w_r$  yields the expression in (18).

**A.4.3. Indirect utility.** To derive the indirect utility, we first compute the (unweighted) average price across all varieties sold in each market. Multiplying both sides of (6) by  $p_{rs}(i)$ , integrating over  $\Omega_{rs}$ , and summing the resulting expressions across  $r$ , we obtain:

$$\bar{p}_s \equiv \frac{1}{N_s^c} \sum_r \int_{\Omega_{rs}} p_{rs}(j) dj = \frac{1}{N_s^c} \sum_r \tau_{rs} w_r \int_{\Omega_{rs}} m_r(j) dj + \frac{\alpha E_s}{N_s^c},$$

where the first term is the average of marginal delivered costs. Under the Pareto distribution,  $\int_{\Omega_{sr}} m_s(j) dj = N_s^E \int_0^{m_{sr}^x} m dG_s(m) = [k/(k+1)] m_{sr}^x N_s^E G_s(m_{sr}^x)$ . Hence, the (unweighted) average price for region  $r$  can be rewritten as follows

$$\bar{p}_r = \frac{1}{N_r^c} \sum_s \tau_{sr} w_s \left( \frac{k}{k+1} \right) m_{sr}^x N_s^E G_s(m_{sr}^x) + \frac{\alpha E_r}{N_r^c} = \left( \frac{k}{k+1} \right) p_r^d + \frac{\alpha E_r}{N_r^c}, \quad (\text{A-8})$$

where we have used (8) and  $p_r^d = \tau_{sr} w_s m_{sr}^x$ . Plugging (A-8) into (4) and using (7), the indirect utility is then given by

$$U_r = \frac{N_r^c}{k+1} - \frac{\alpha}{\tau_{rr} m_r^d}, \quad (\text{A-9})$$

which, together with (17) and (18), yields (20).